

Kent Irwin, NIST

## Readout of Large Format Microcalorimeters

### Some examples of microcalorimeters

- Transition-edge sensors (TES)
- Magnetically coupled calorimeters (MCC)
- Microwave kinetic inductance detectors (MKID) when run in a thermal mode

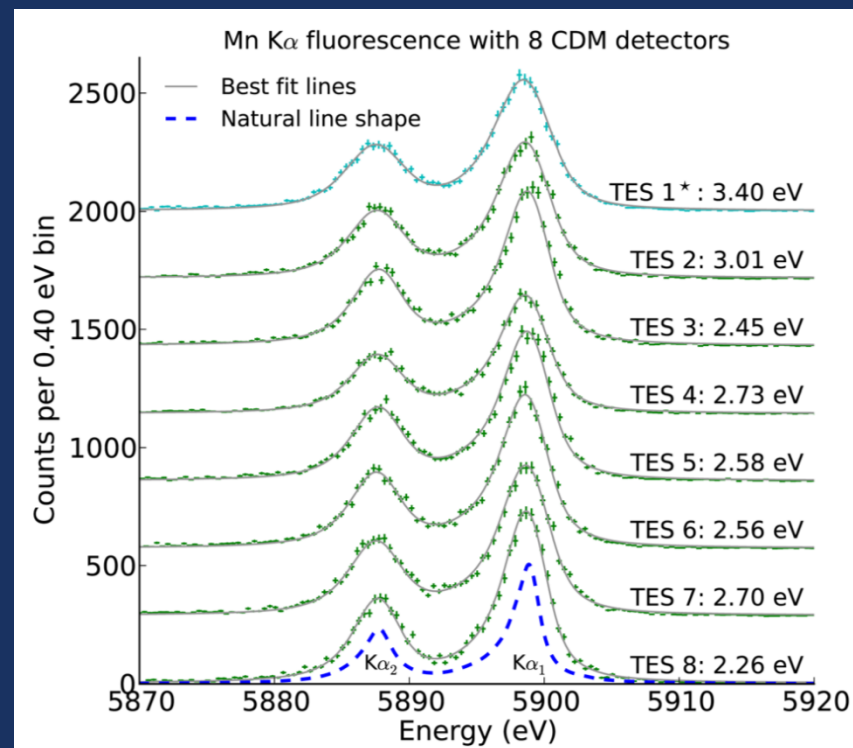
### Outline: a roadmap for readout

Moore's Law curves for pixel count

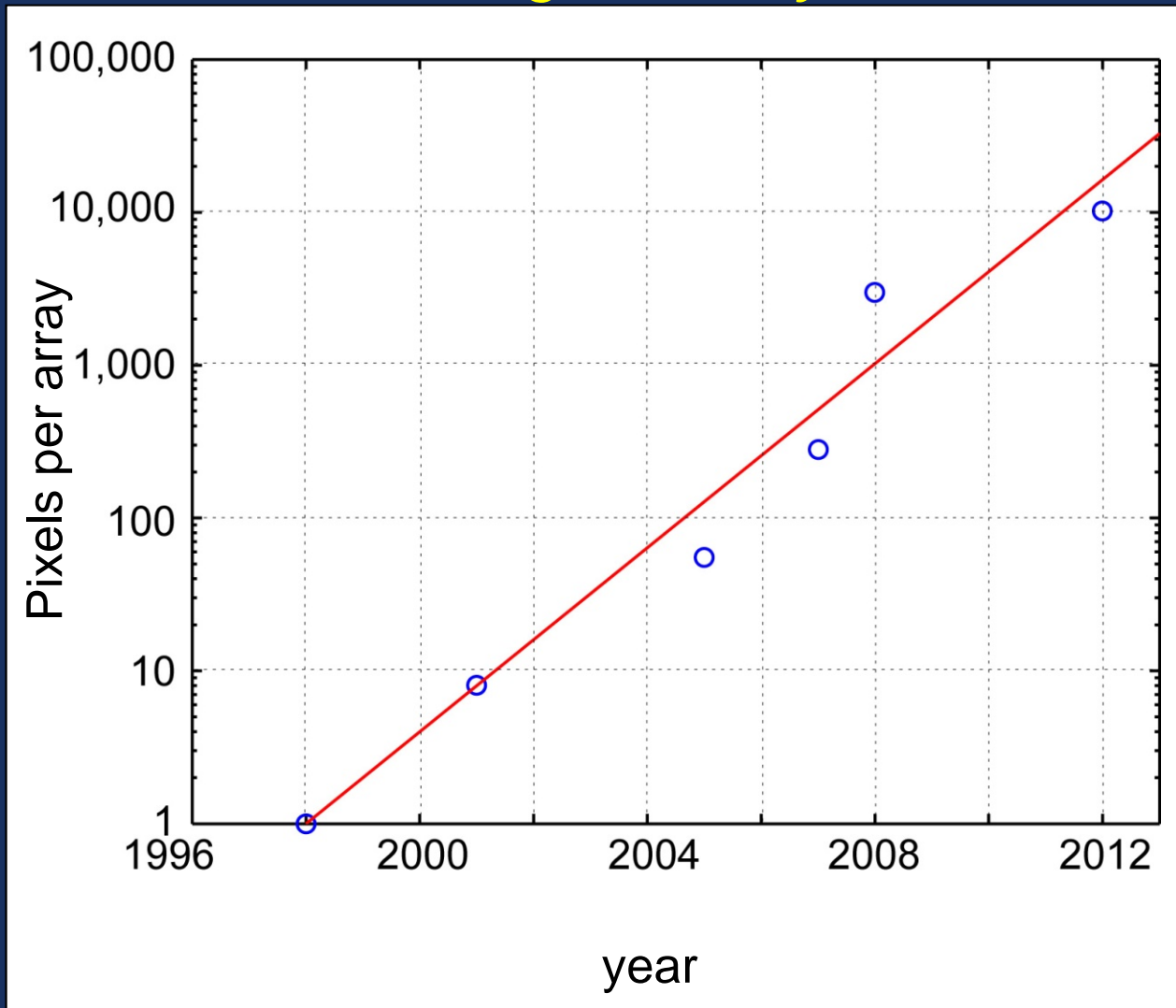
Shannon limits: we are nowhere near them

Multiplexing: FDM, TDM, CDM

Bandwidth: MHz or GHz



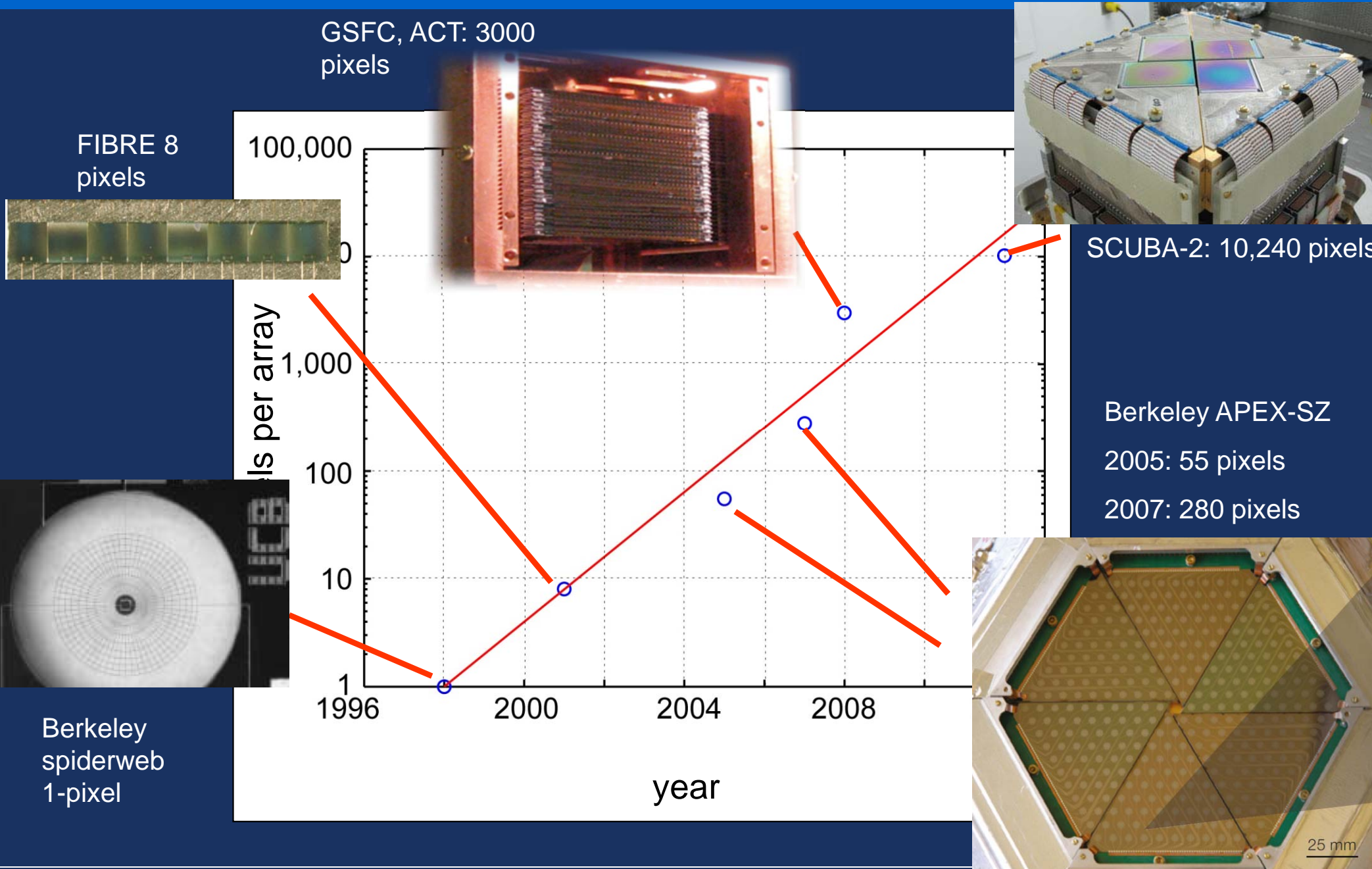
*Doubling time: 1 year*



Easy: low dynamic range

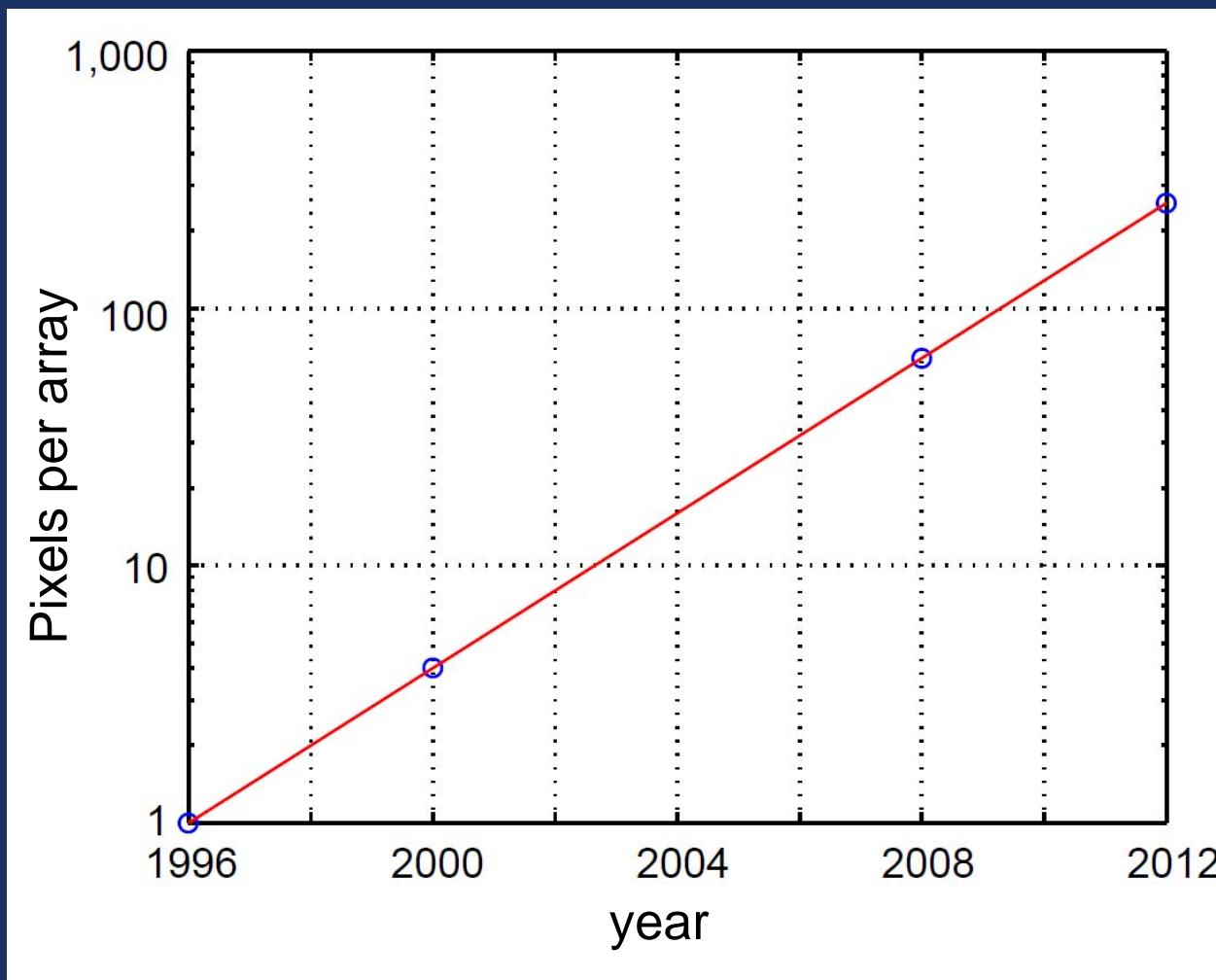
Megapixel by 2020

# Moore's law for TES bolometers



# Moore's law for instrumented *x-ray* TES calorimeters

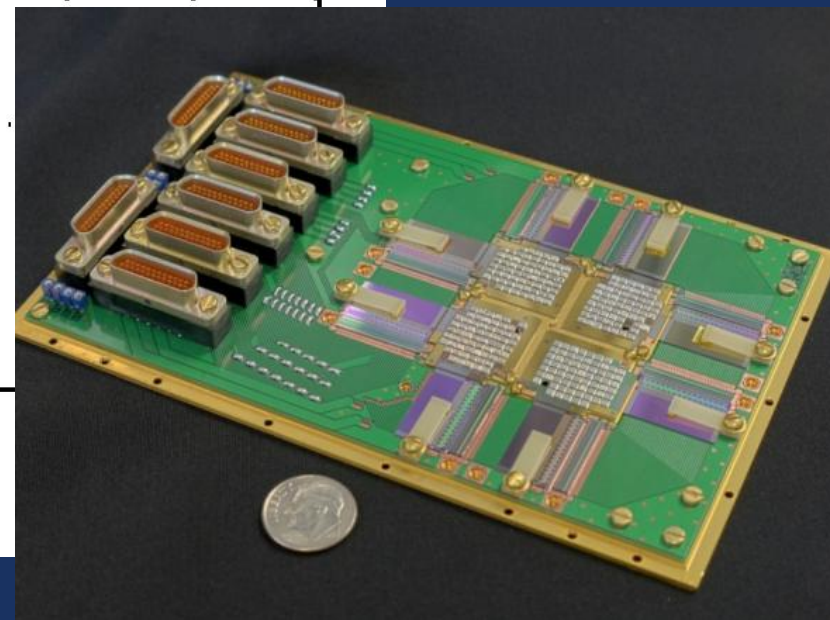
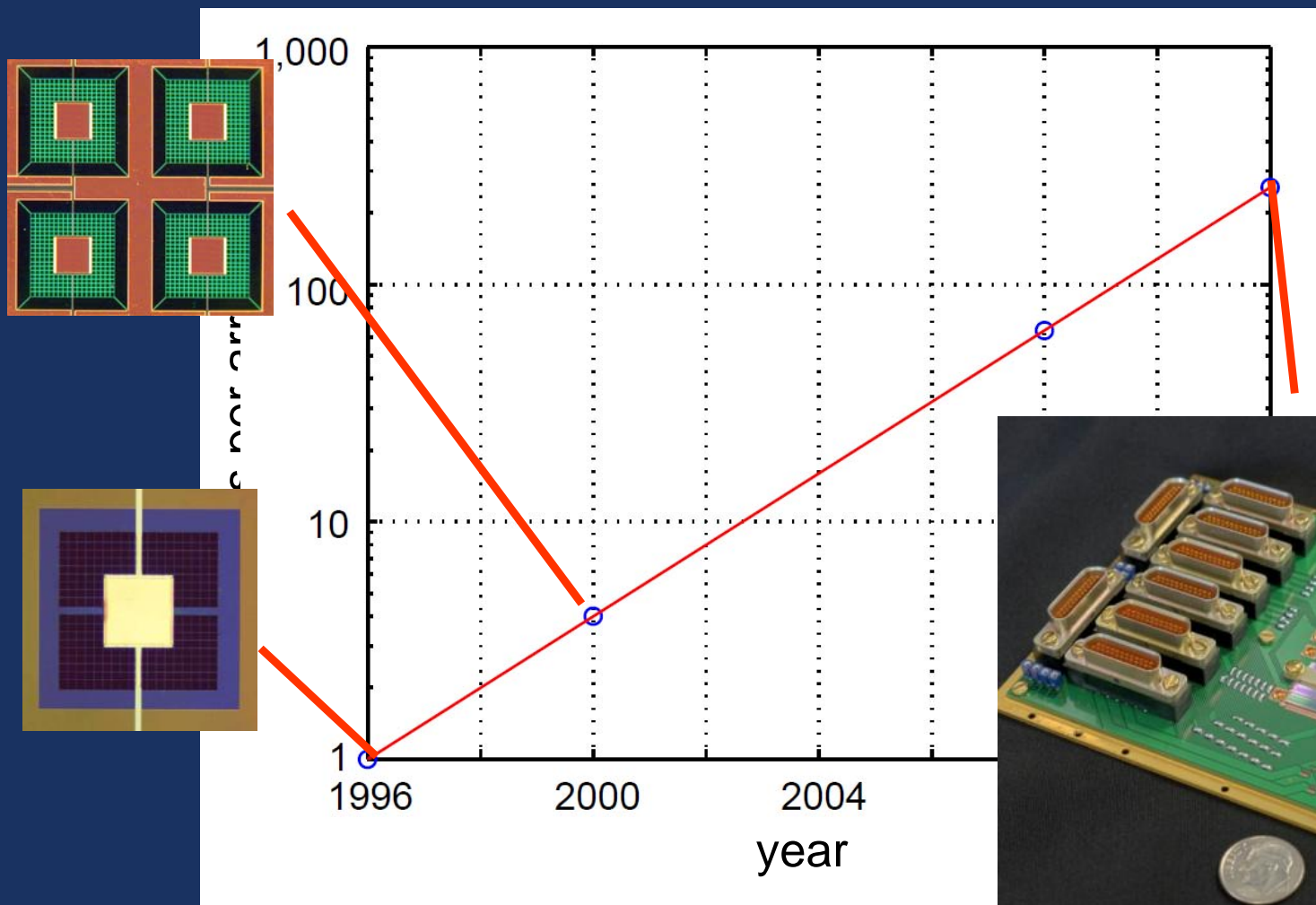
*Doubling time: 2 years*



Much harder  
because of  
dynamic range  
of x-ray events

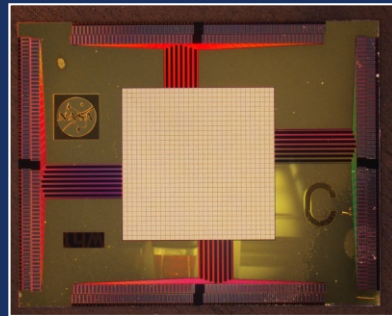


# Moore's law for instrumented *x-ray* TES calorimeters



# Moore's law: the next $\times 1000$

*Doubling time: 2 years*



4. TES or MCC with GHz FDM + CDM

3. TES or MCC or MKID with GHz FDM

2. TES with CDM

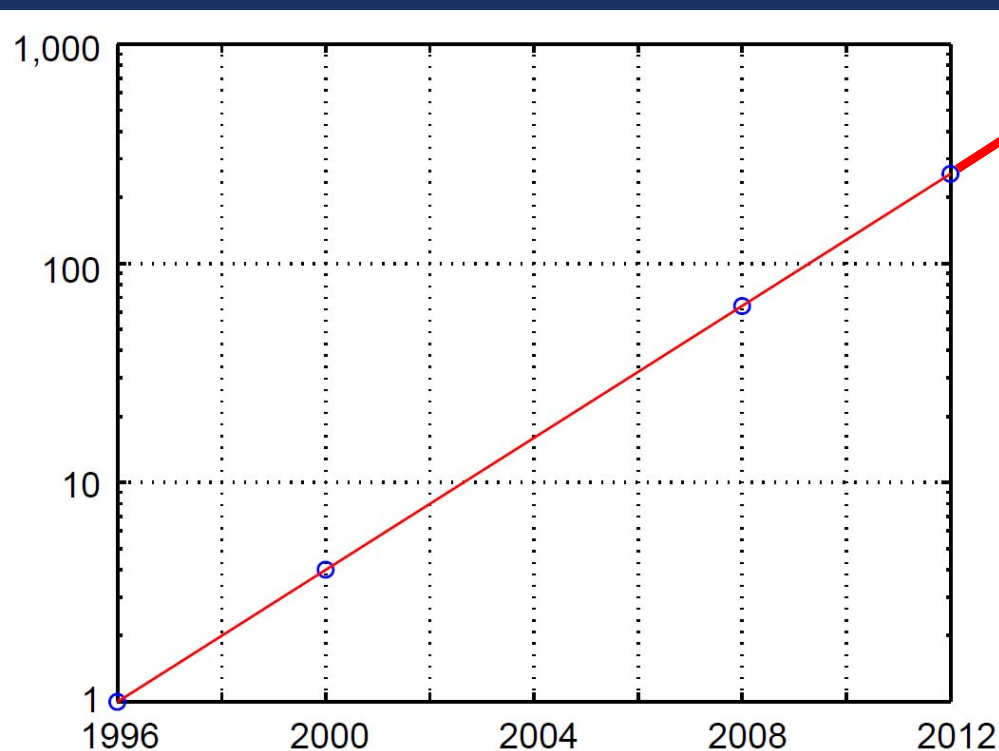
1. TES with TDM

field of view

TRADE OFF

resolution

speed



X-ray SAG, Monterey, 2013

# What is the limit? How many can we mux?

- To fully characterize a signal with bandwidth  $B$ , it must be sampled at the “Nyquist rate”

$$\Delta t_{NYQ} = \frac{1}{2B}$$

The Nyquist-Shannon Sampling Theorem

- The number of voltage levels that can be distinguished in each sample is determined by the signal-to-noise ratio. The number of bits of information scales as  $\log_2$  of the number of distinguishable voltage levels.
- Taken together, the number of bits per second in an analog communication channel is:

$$C = B \log_2 \left( 1 + (S/N)^2 \right) \quad \text{The Shannon-Hartley Theorem}$$

# Megapixel arrays are possible

## SQUID

$$\Delta\Phi = \Phi_0$$

$$\Phi_n = 1\mu\Phi_0 / \sqrt{\text{Hz}}$$

$$B = 1 \text{ MHz}$$

$$C = 20 \text{ MHz}$$

## HEMT + coax

$$\Delta P \sim -40 \text{ dBm}$$

$$P_n = -90 \text{ dBm}$$

$$B = 10 \text{ GHz}$$

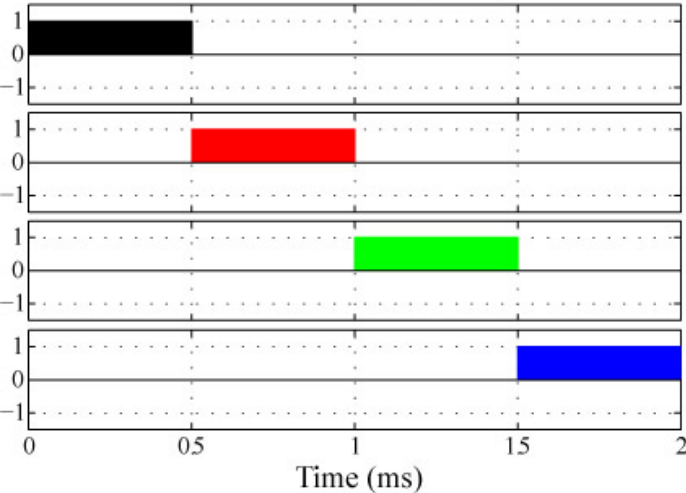
$$C = 175 \text{ GHz}$$

With perfect “Shannon efficiency” we could read out hundreds of detectors per MHz SQUID, or millions per HEMT

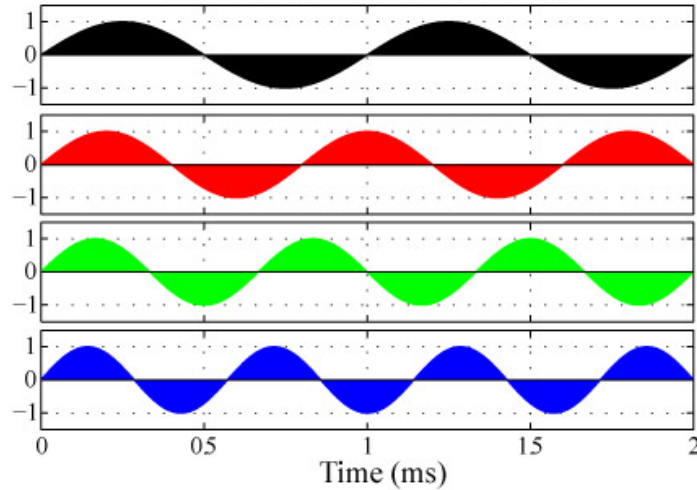


# How to mux: three modulation functions

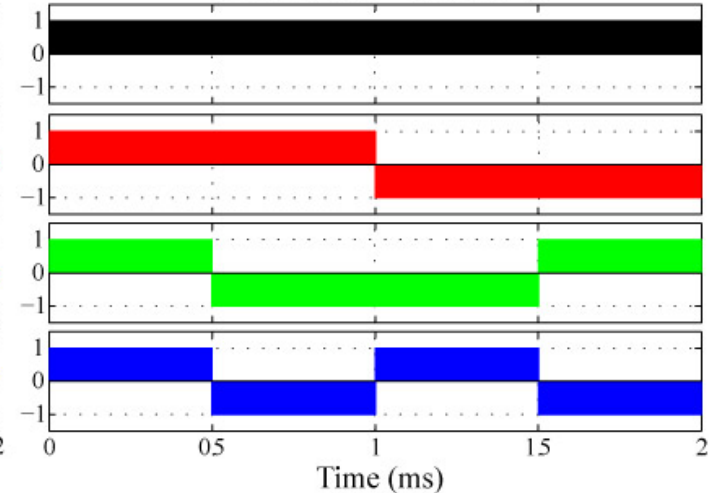
## Time-division MUX



## Frequency-division MUX



## Code-division MUX



- Define time band by coupling output 'channel' to different detectors sequentially.

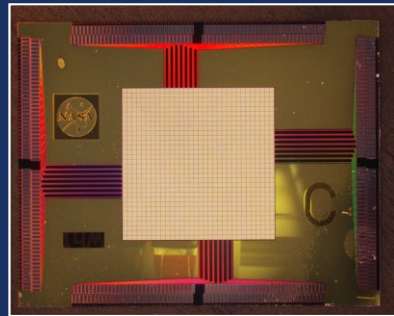
- Define frequency band with different passive LC circuits

- Define 'code' band by switching the polarity with which each detector couples to the output channel in an orthogonal Walsh pattern



# Moore's law: the next $\times 1000$

*Doubling time: 2 years*



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2. TES with CDM

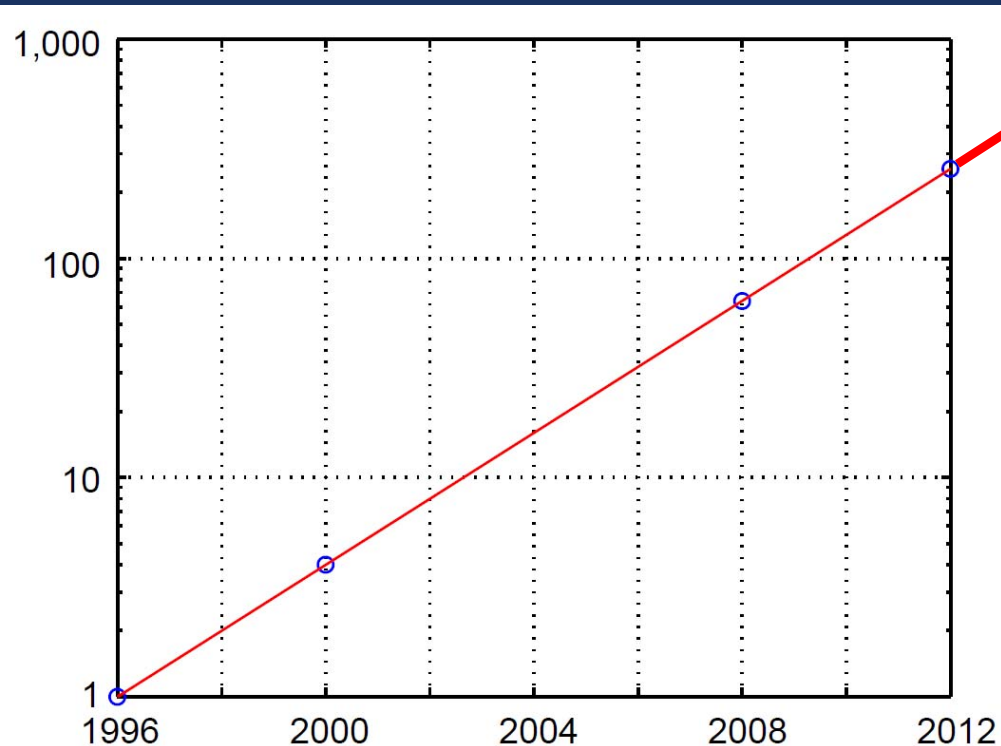
1. TES with TDM

field of view

TRADE OFF

resolution

speed



X-ray SAG, Monterey, 2013

NIST

# TDM of XMS baseline

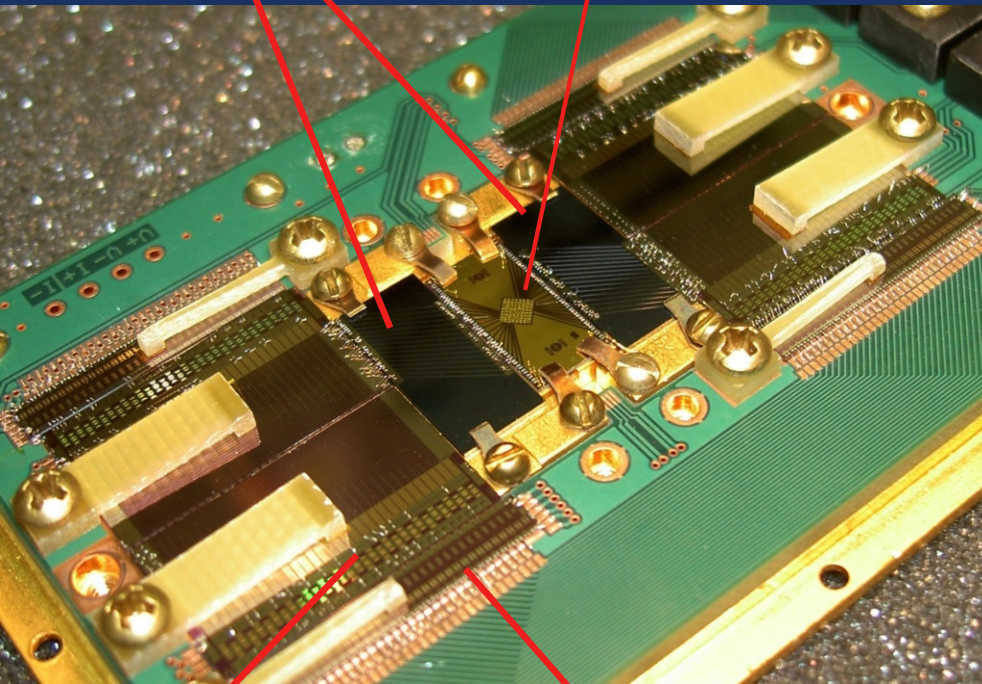
GSFC 8 x 8 array  
NIST SQUID MUX readout

2 x 8 mux readout of 8x8 array

$$\Delta E_{\text{FWHM}} = 2.9 \text{ eV}$$

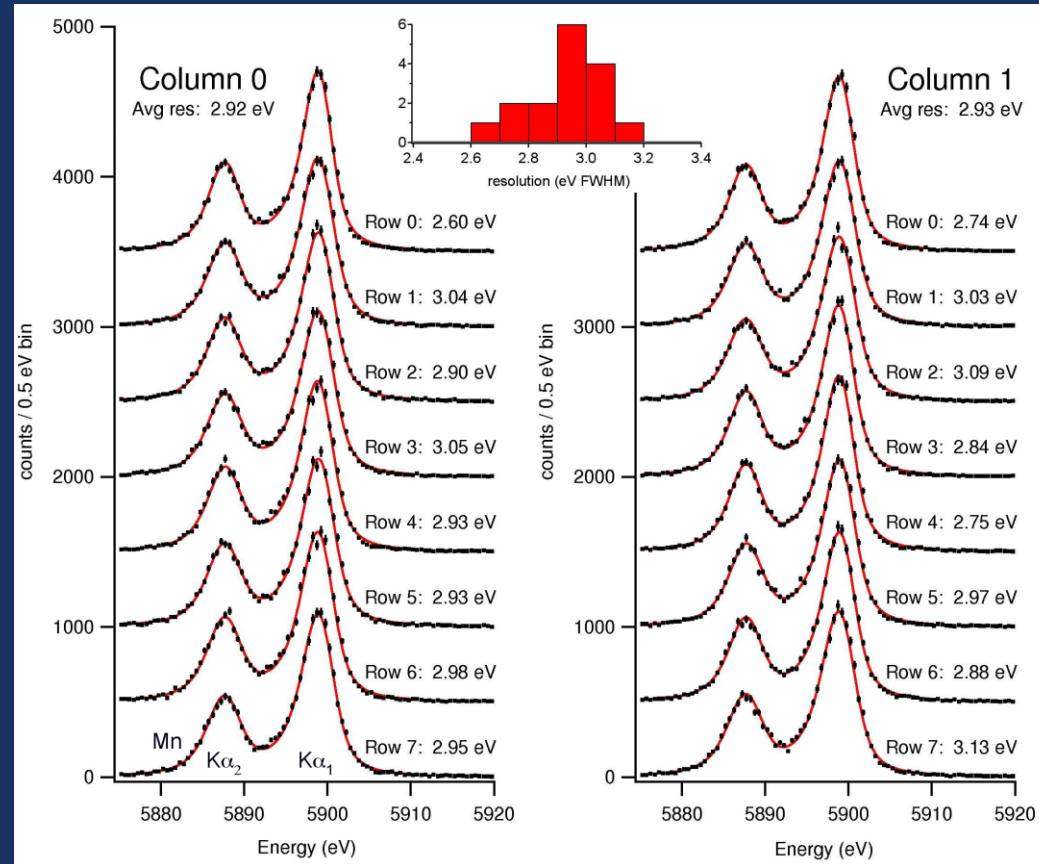
Interface chips

Calorimeter array



Anti-alias filters +  
TES bias resistors

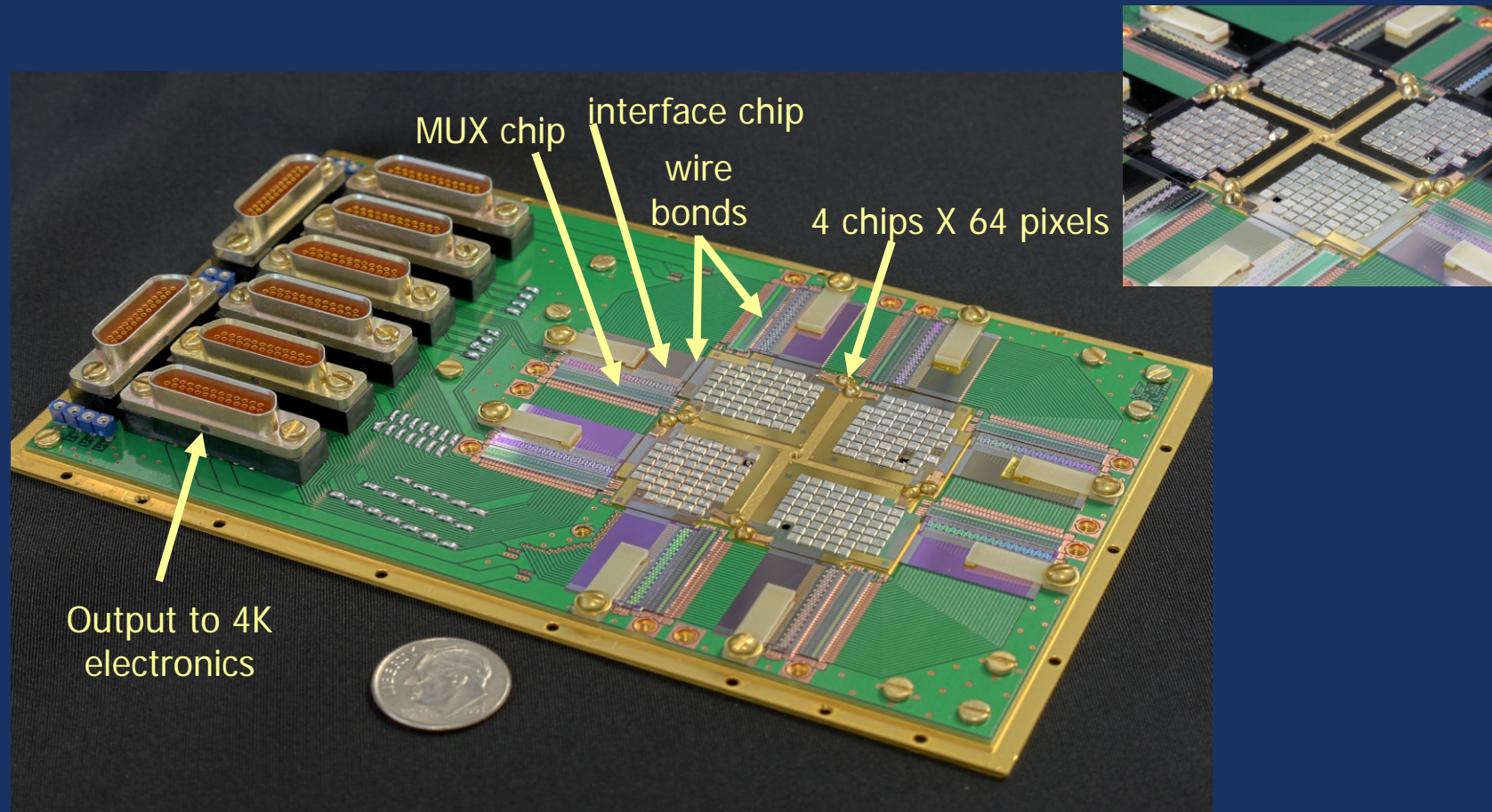
SQUID  
multiplexers





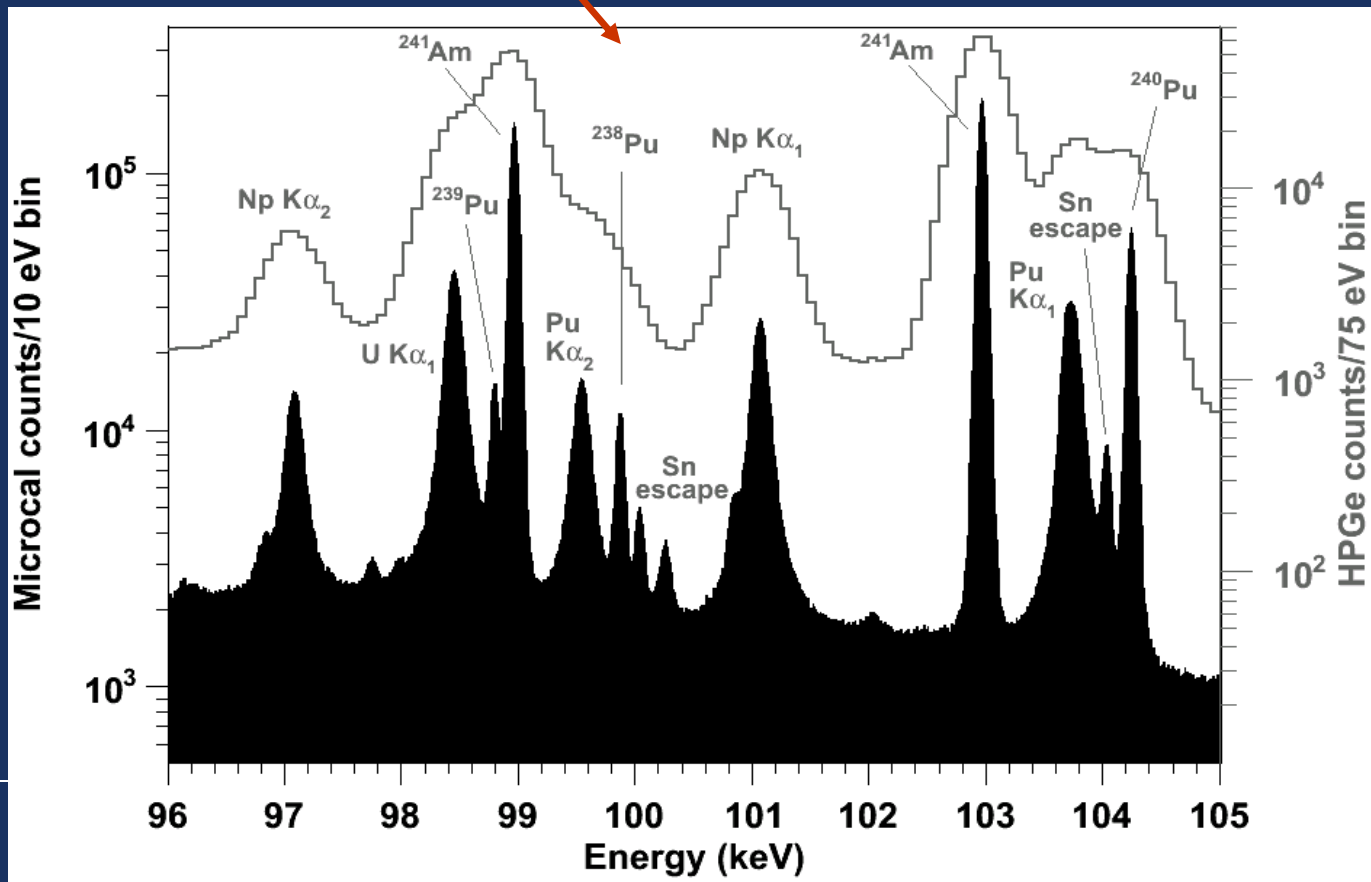
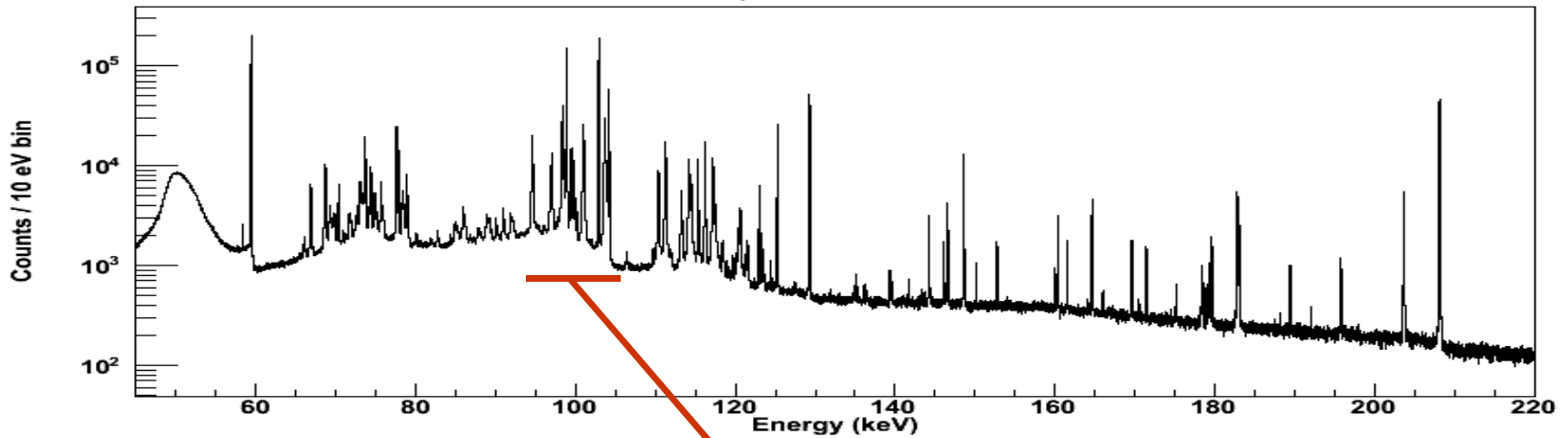
# Largest instrumented microcalorimeter: 256 pixel hard x-ray array

- 8x32 readout architecture
- total collection area = 576 mm<sup>2</sup> (planar HPGE ~200-1000 mm<sup>2</sup>)



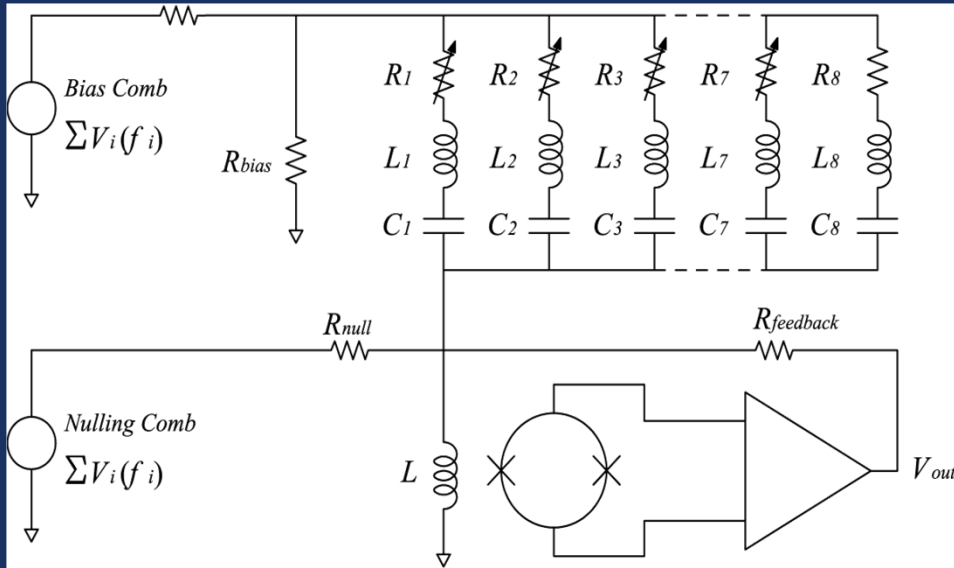
# Hard x-ray array: mixed nuclear isotope spectrum

Microcal PIDIE-3 spectrum with 30 million counts





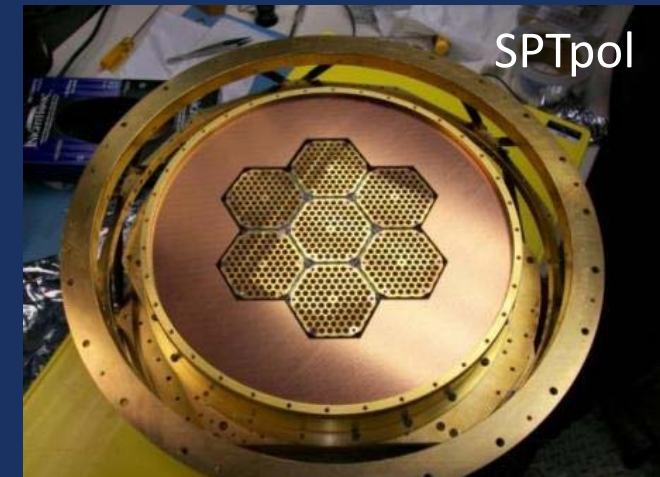
# FDM with bias modulation: *bolometers, not (yet) calorimeters*



SRON, ESA, Japan:  
SAFARI instrument for SPICA

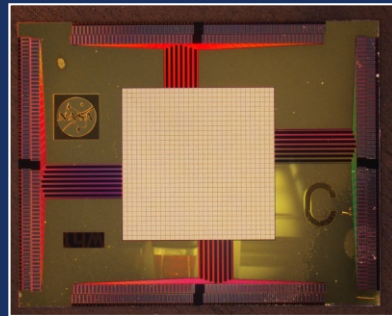
But, AC-modulating TES  
calorimeters is observed to  
degrade energy resolution  
significantly

Fielded experiments using FDM: Berkeley, LBNL, McGill electronics, NIST SQUIDs & inductors



# Moore's law: the next $\times 1000$

*Doubling time: 2 years*



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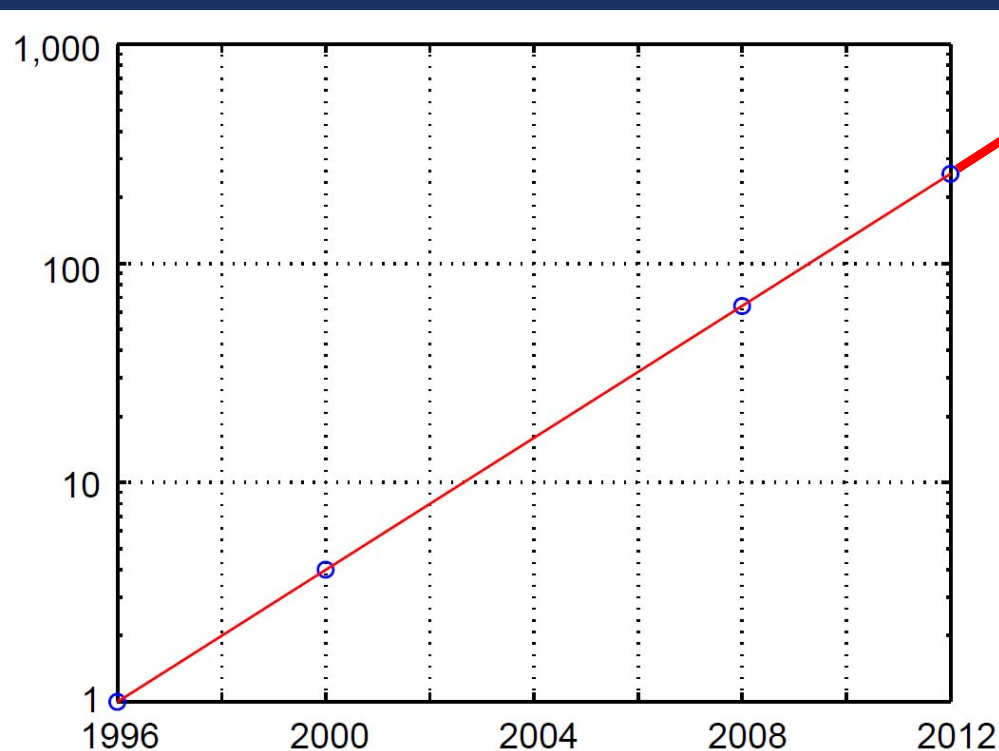
1. TES with TDM

field of view

TRADE OFF

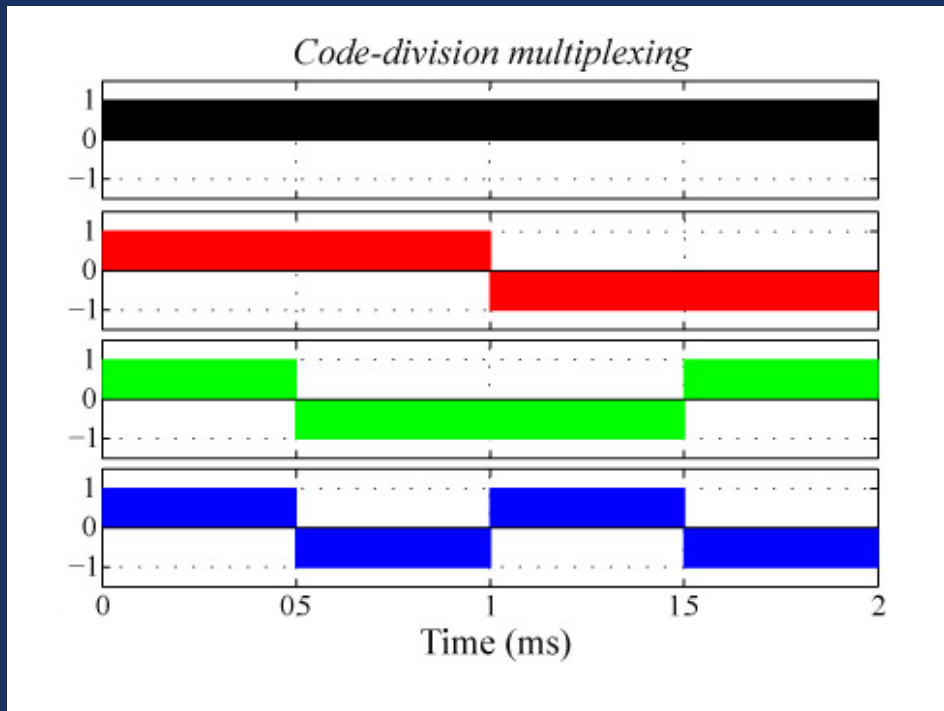
resolution

speed



X-ray SAG, Monterey, 2013

# CDM: better dynamic range, energy resolution than TDM



- Every detector pixel is on all of the time
- Polarity of coupling to the output switches between +1 and -1 in orthogonal pattern (Walsh matrix)
- Original signals recovered by multiplying by inverse Walsh matrix.
- Does not have “multiplex disadvantage” that exists for TDM multiplexing

$$\begin{pmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \\ 1 & -1 & 1 & -1 \end{pmatrix}^{-1} = \frac{1}{4} \begin{pmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \\ 1 & -1 & 1 & -1 \end{pmatrix}$$

Additional benefit: SQUID 1/f noise and common-mode rf pickup is removed in all but the first (non-switching) row

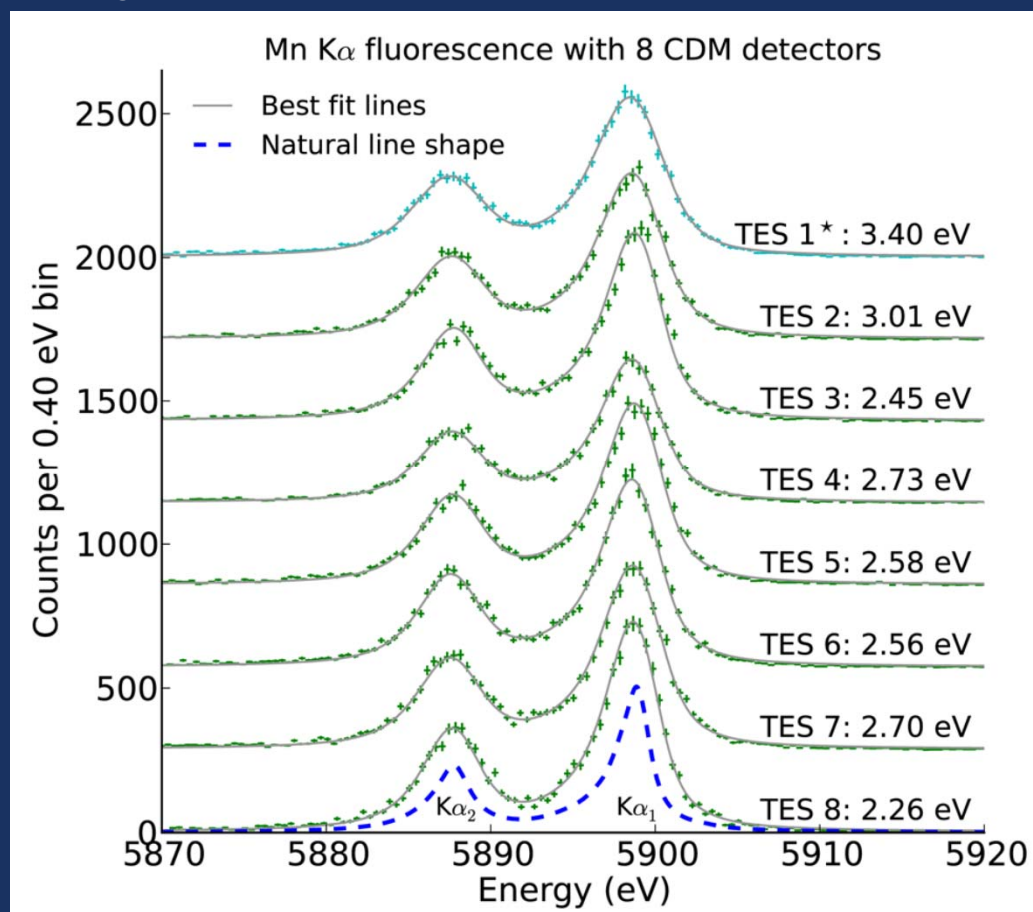
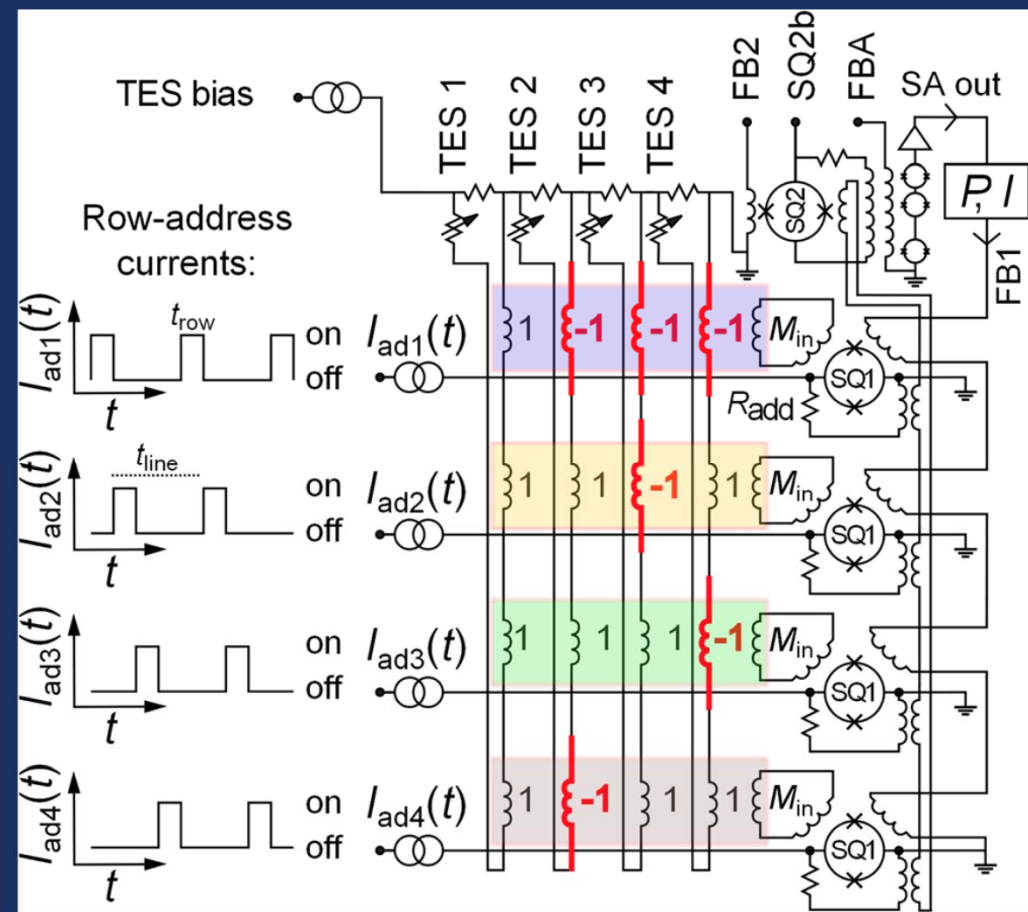
# CDM: excellent performance demonstrated

CDM chips are drop-in compatible with existing 32-row TDM systems, with the same wiring and readout electronics, but have higher performance.

$$\Delta E_{\text{FWHM}} = 2.58 \text{ eV FWHM at } 5.9 \text{ keV (unswitched pixel excluded)}$$

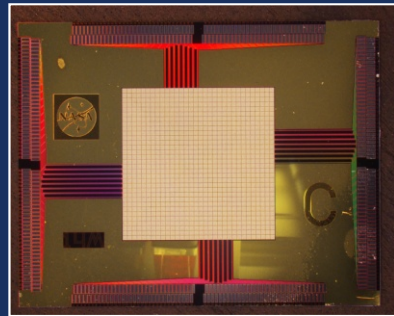
*Circuit (flux coupled CDM):*

*Promising first results from 1x8 CDM demonstration:*



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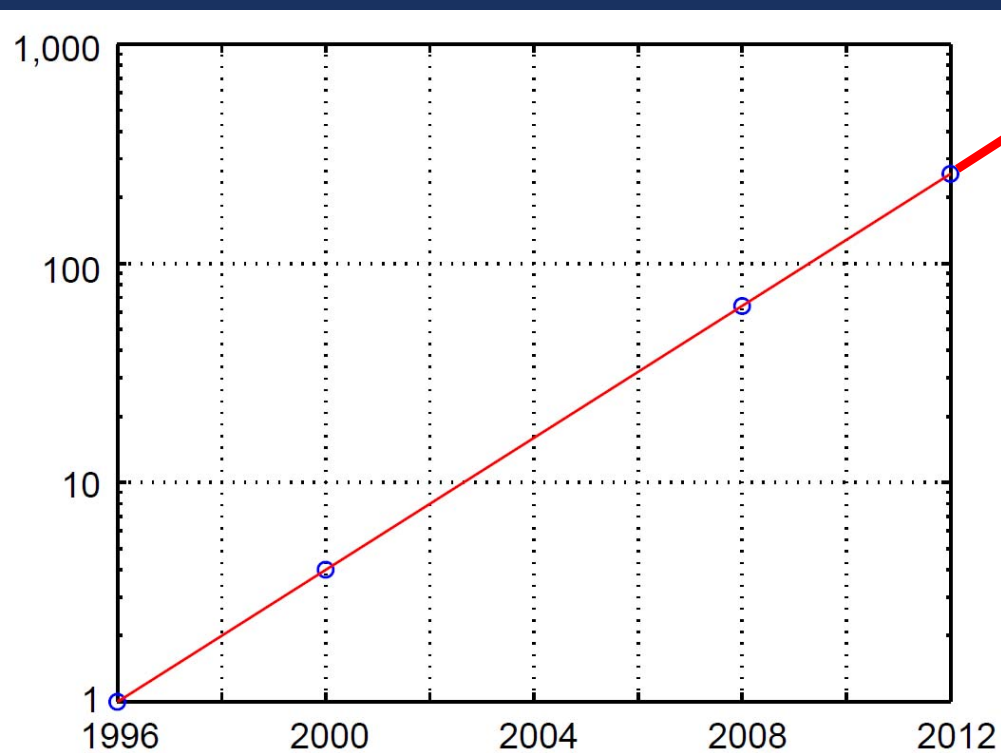
1. TES with TDM

field of view

TRADE OFF

resolution

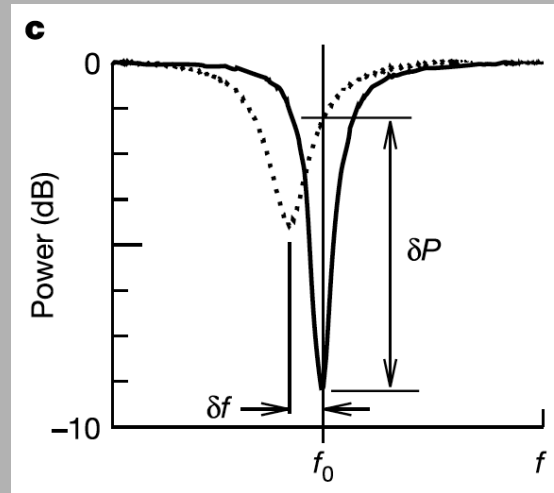
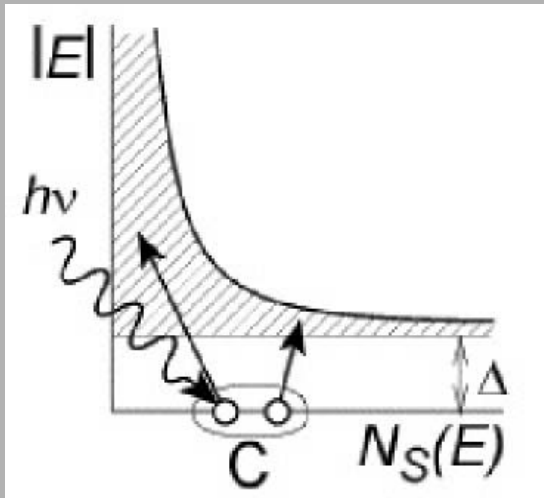
speed





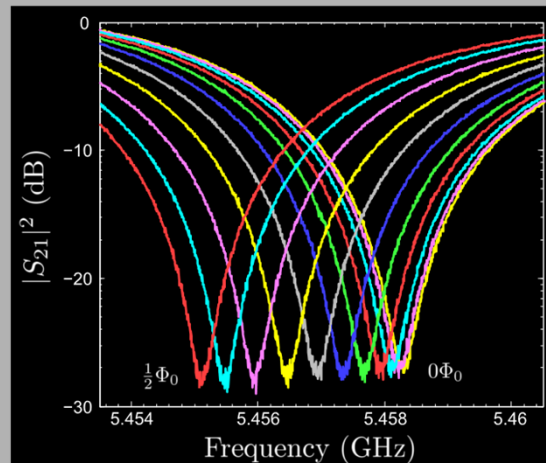
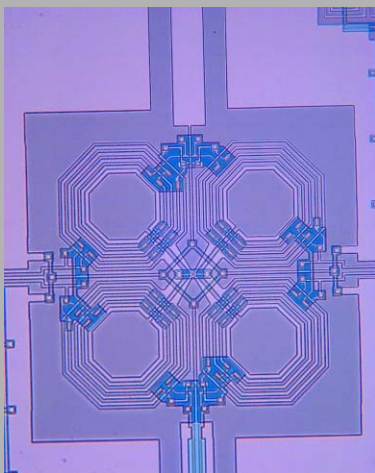
# GHz FDM multiplexing convergence

Microwave kinetic inductance detectors (MKIDs): detector is resonator



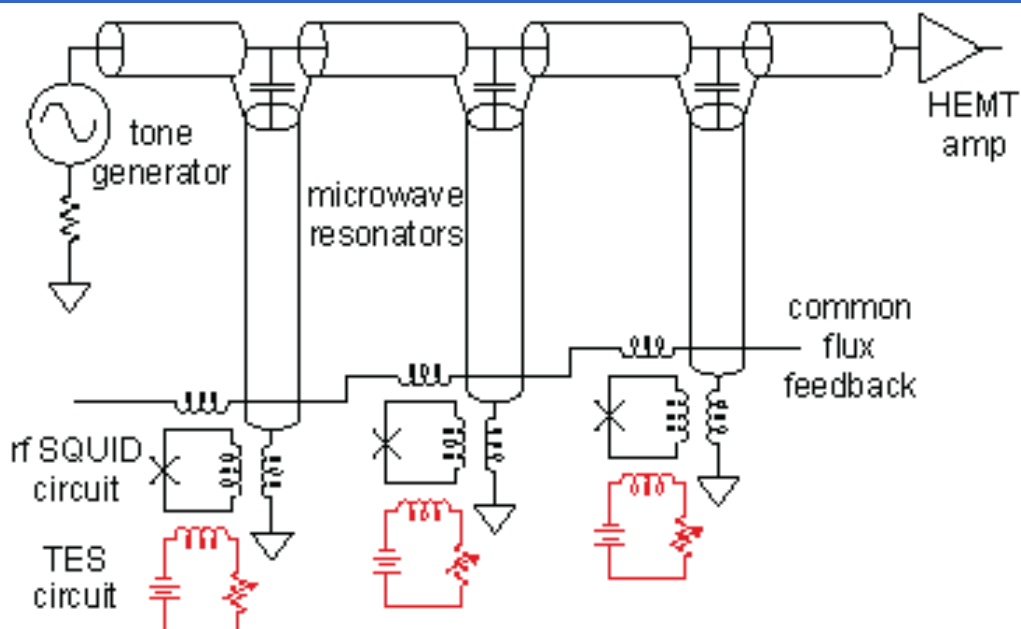
- Single pixel x-ray performance needs to be demonstrated
- P. Day, Nature (2003)

TES detectors or MMCs coupled to microwave resonators



- Dissipationless SQUID in each resonator
- B. Mates, Appl. Phys. Lett. (2008)

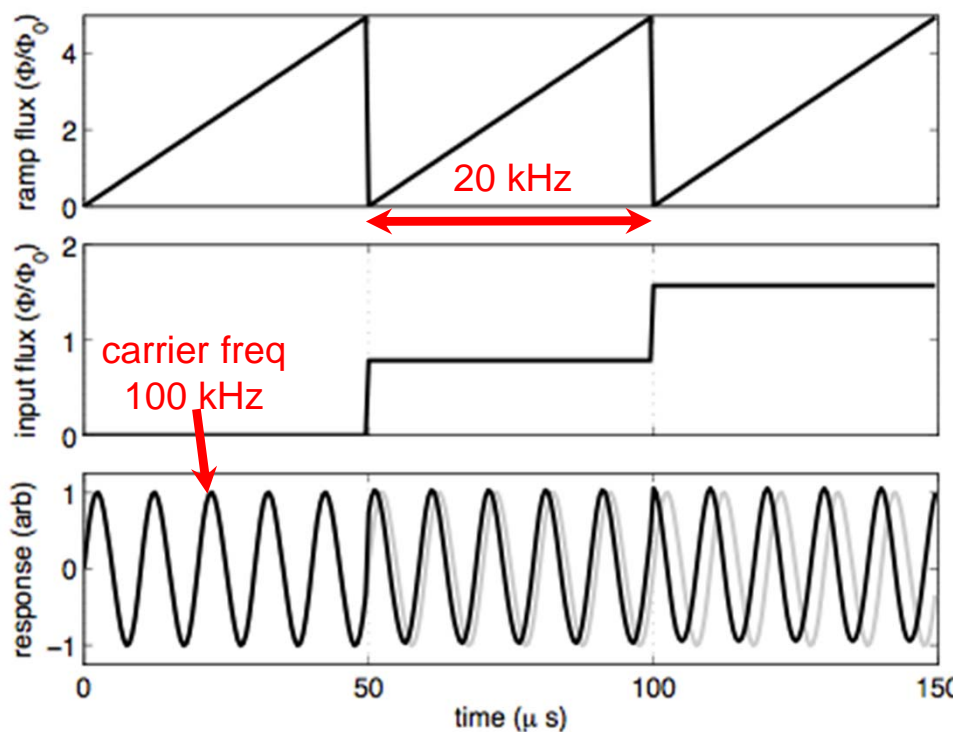
# GHz resonators for TES / MCC microcalorimeters



Array has:  
2 coaxes (1 input + 1 output,  
like MKIDs)

2 low-frequency lines (1 dc  
bias, 1 flux ramp)

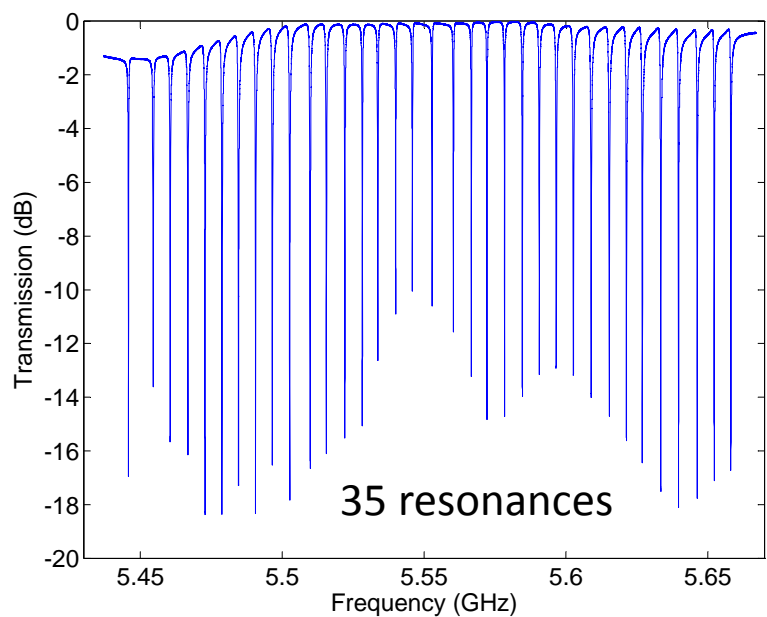
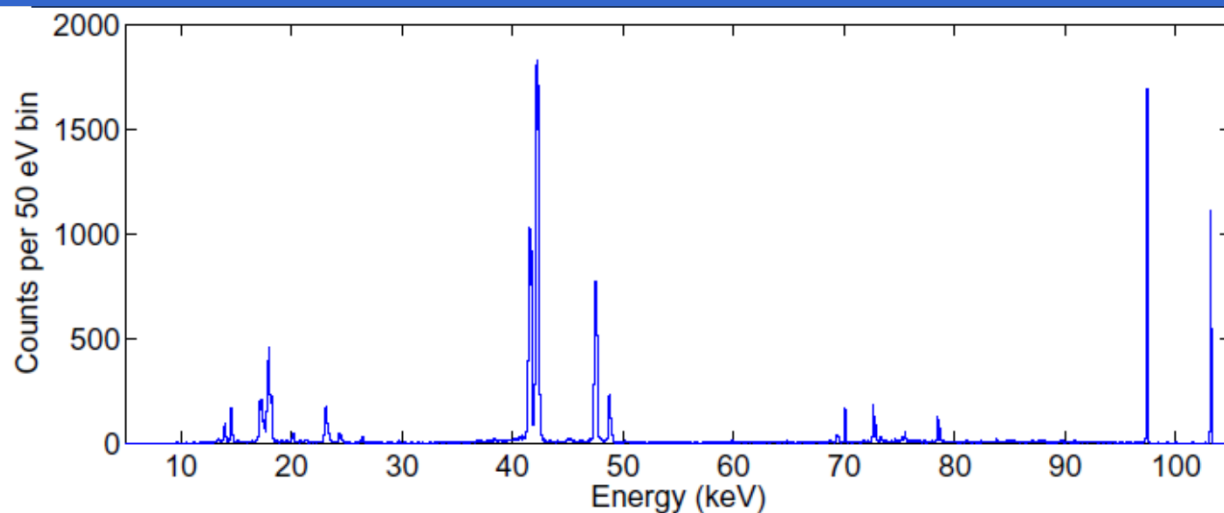
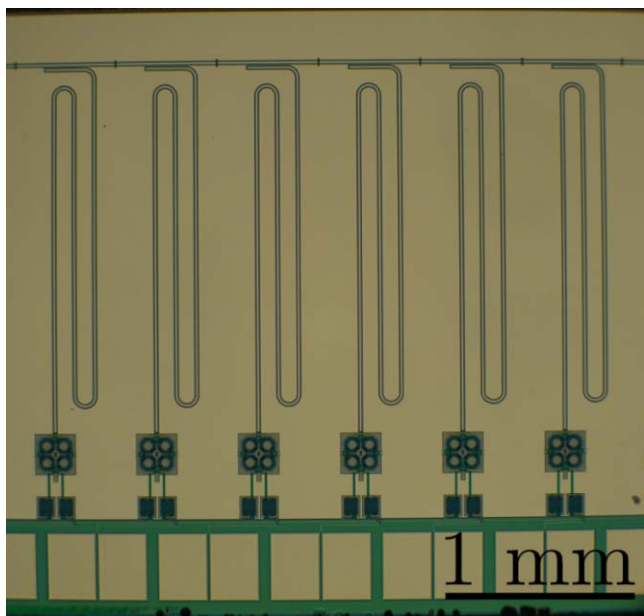
FLUX RAMP



SIGNAL

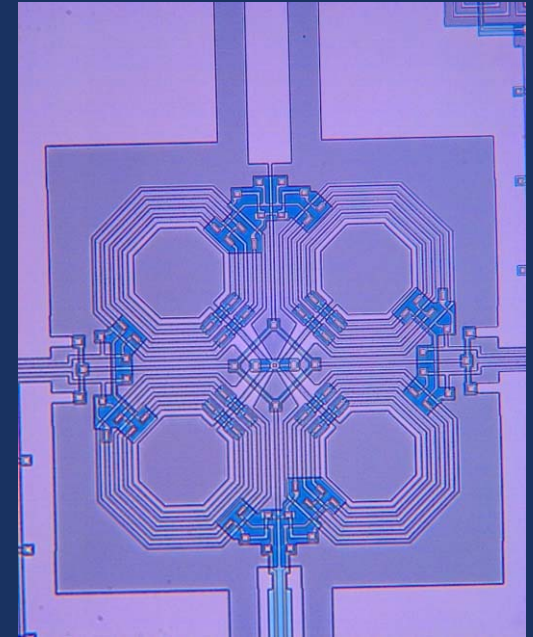
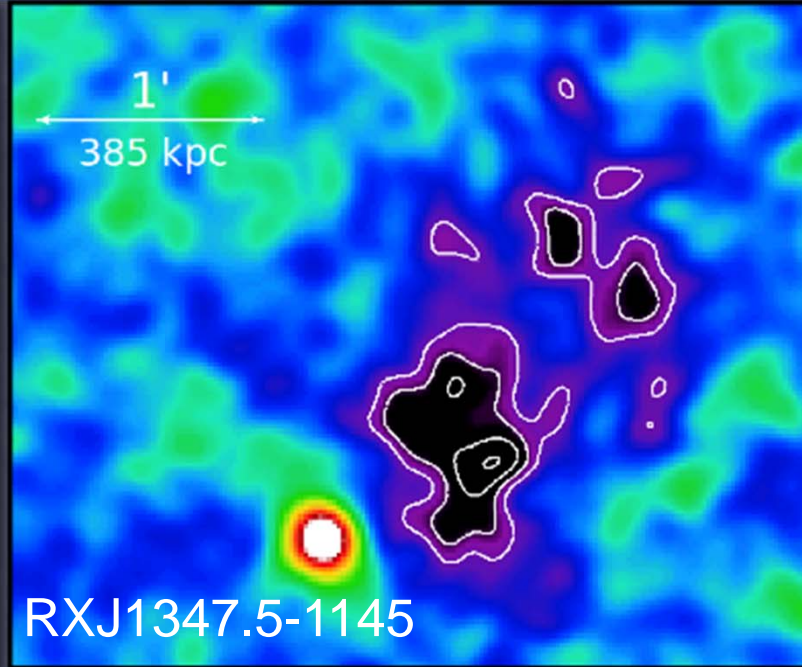
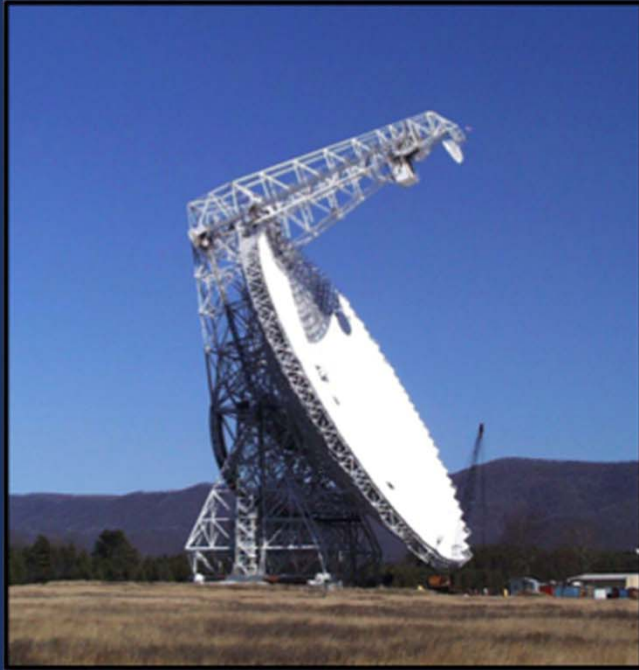
Output

# First GHz FDM x-ray demonstration with high spectral resolution



- Spectrum of Gd-153 with TES hard x-ray calorimeters
- At 100 keV, energy resolution ( $E/\Delta E_{\text{FWHM}} \sim 1500$ ) very close to the unmultiplexed value
- Two pixels demonstration conducted with rack-mount hardware; large-format electronics compatible with x-ray dynamic range pending

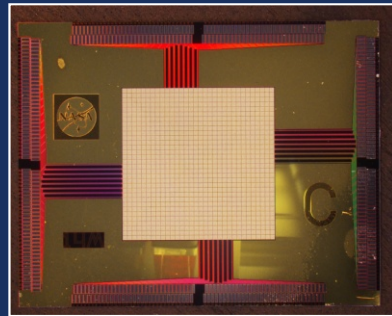
# First GHz multiplexed TES bolometer on the sky: MUSTANG 2



- MUltiplexed SQUID TES Array at Ninety GHz
- High-resolution (9'') Sunyaev-Zel'dovich follow up at 90 GHz
- 100 m Green Bank Telescope
- 383 feedhorn (1.9 f $\lambda$ ) TESs
- Read out with ROACH + ARCONS/MUSIC

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*Doubling time: 2 years*



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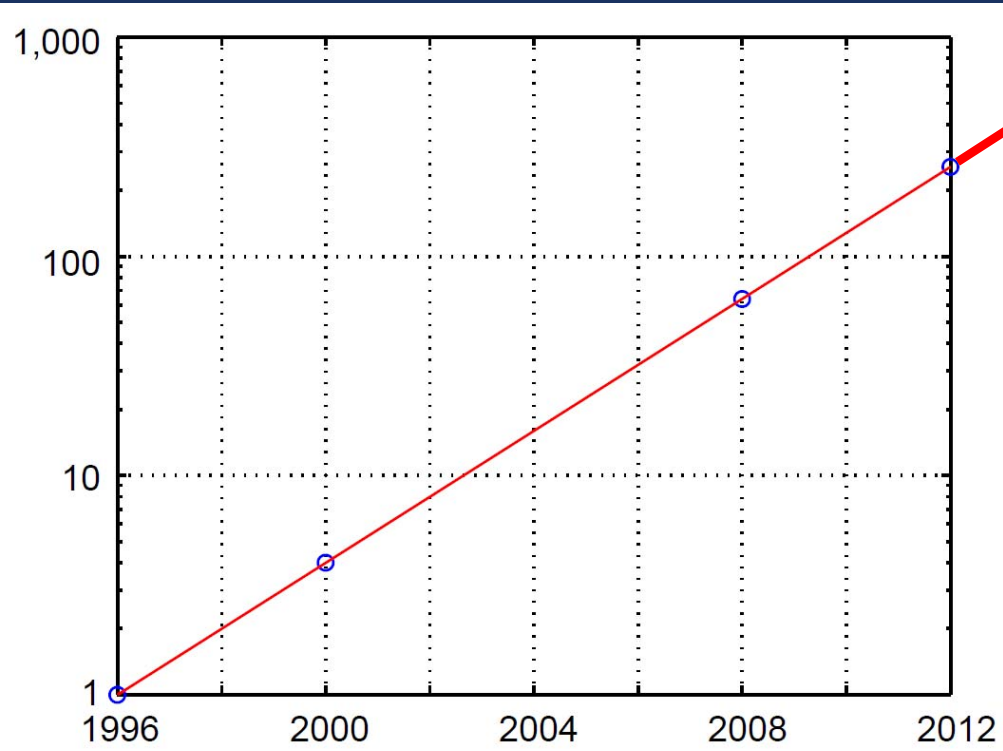
1. TES with TDM

field of view

TRADE OFF

resolution

speed



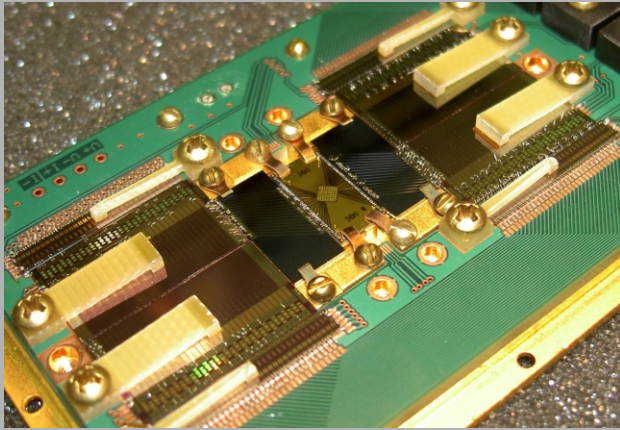
X-ray SAG, Monterey, 2013





# Three tiers of array scale

MHz mux  
(TDM, FDM, CDM TES)

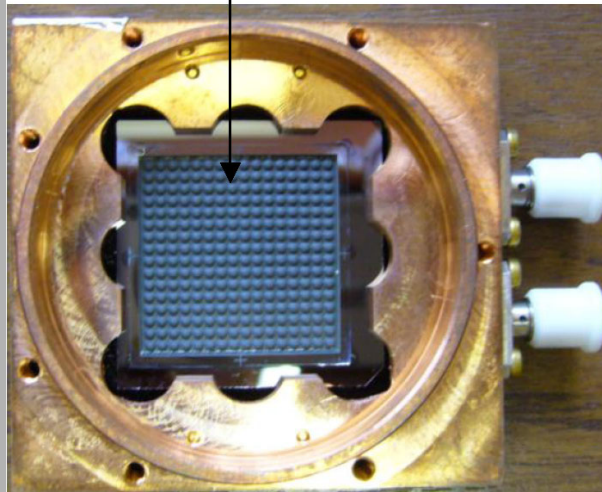


XMS x-ray prototype

- High Shannon efficiency
- MHz bandwidth / channel
- $\sim 10^4$  pixels

GHz mux  
(MKID, TES)

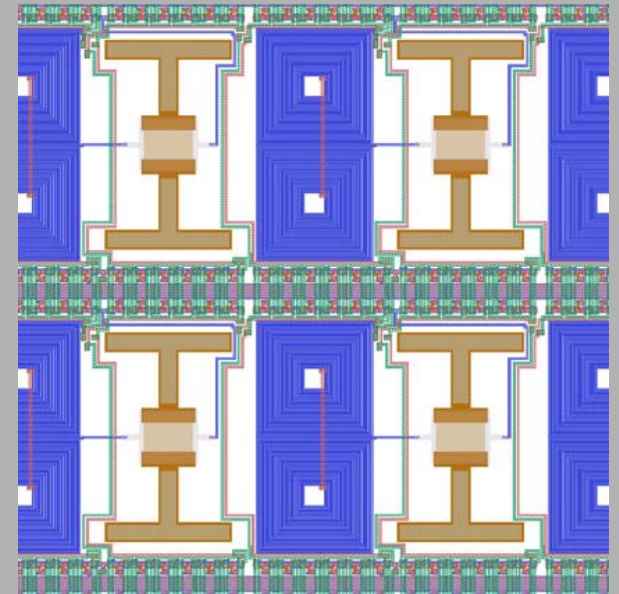
$\lambda/4$  waveguide resonator, Twin-slot antenna, 1.6mm Si micro-lenses



NIKA submm array

- Low Shannon efficiency
- GHz bandwidth / channel
- $\sim 10^5$  pixels

hybrid GHz mux  
(resonator + CDM)

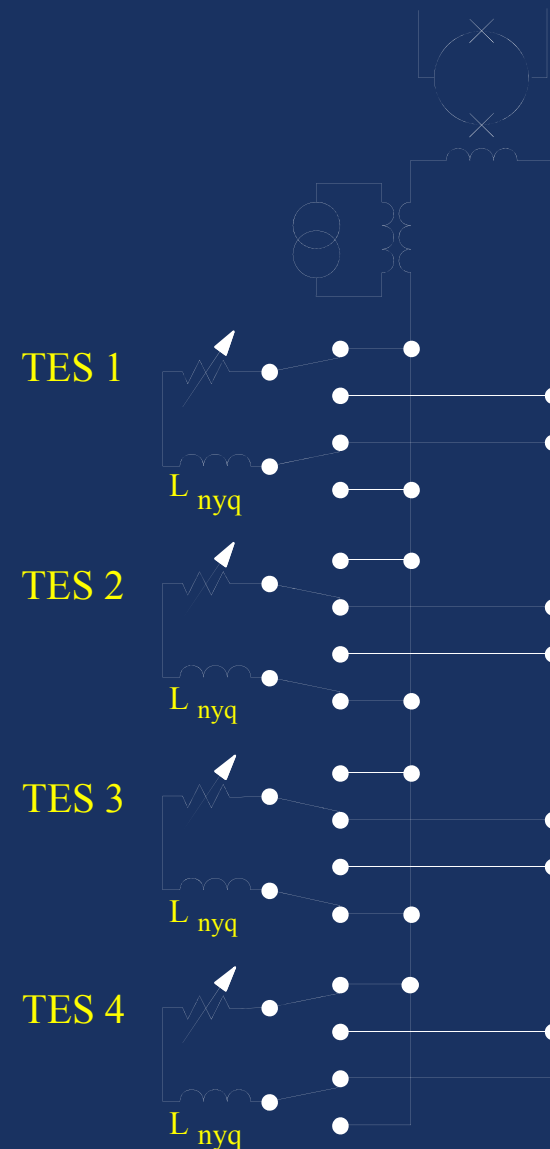


Hybrid design

- High Shannon efficiency
- GHz bandwidth / channel
- $\sim 10^6$  pixels

# Hybrid circuit: hundreds of detectors per resonator

- Current from all calorimeters is summed in one output resonator
- Polarity with which each calorimeter couples to the output SQUID is switched in Walsh code
- No TES shunt resistors or power
- Compact modulation elements (*much* smaller than resonators / MKIDSs)



# Design for 300 $\mu\text{m}$ hybrid x-ray pixel

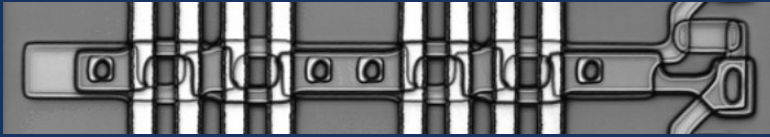


Photo: I-CDM modulator

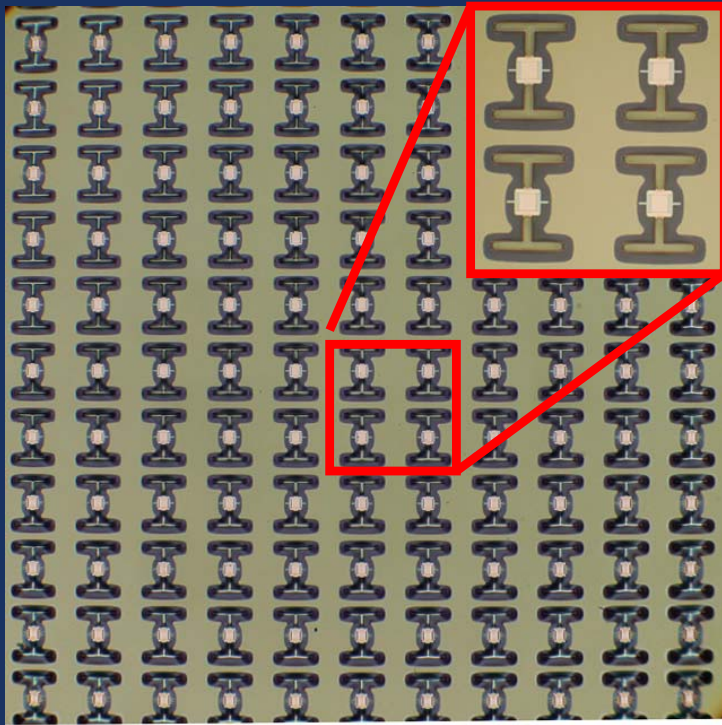
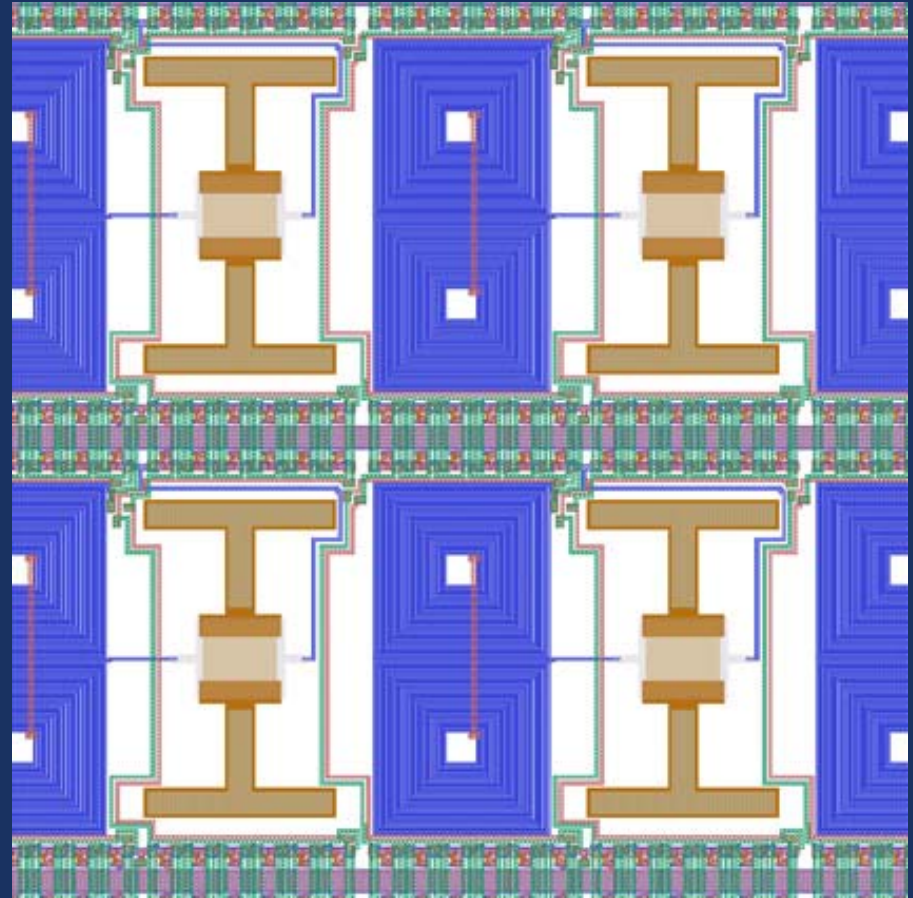


Photo of  $32 \times 32$  array of x-ray calorimeters on 300  $\mu\text{m}$  pitch – D. Schmidt



Lithographic layout of in-focal-plane I-CDM modulators on 300  $\mu\text{m}$  pitch

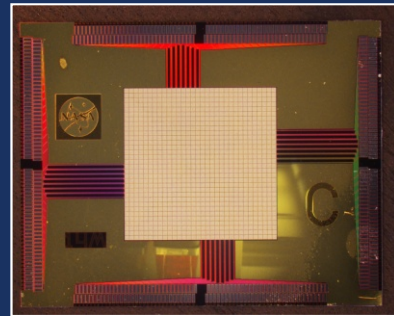
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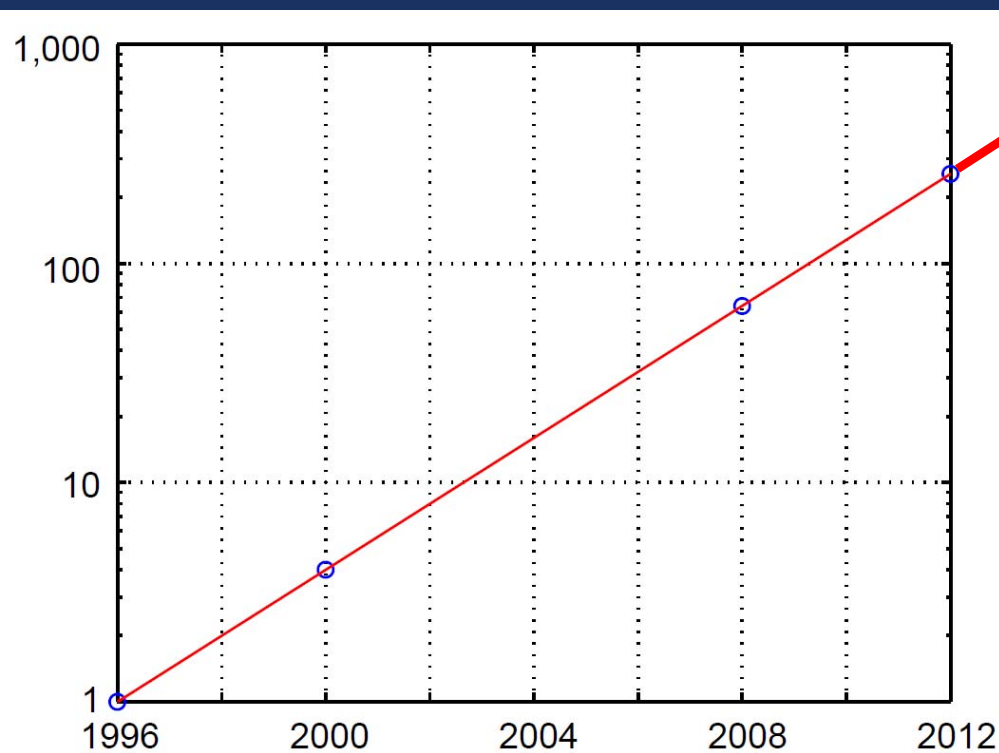


field of view

TRADE  
OFF

resolution

speed



X-ray SAG, Monterey, 2013

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