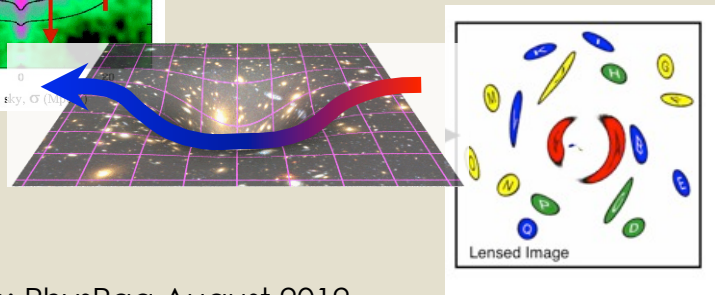
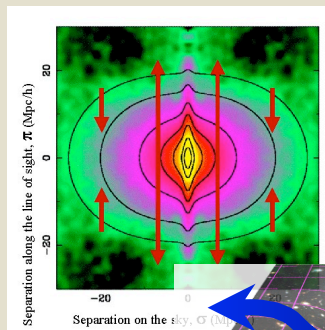


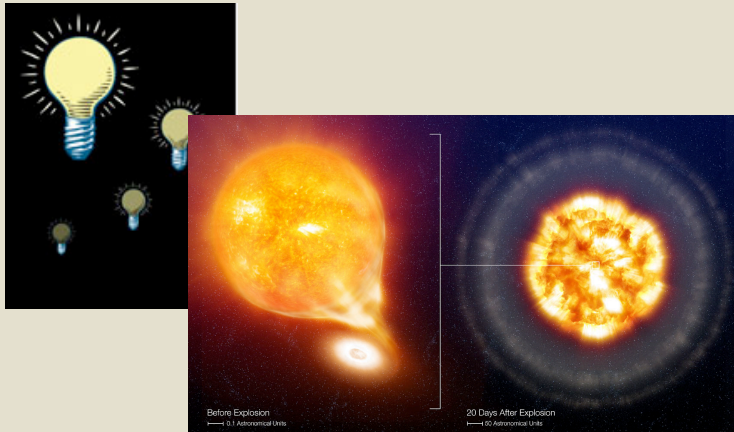
Understanding dark energy

Rachel Bean
Cornell University

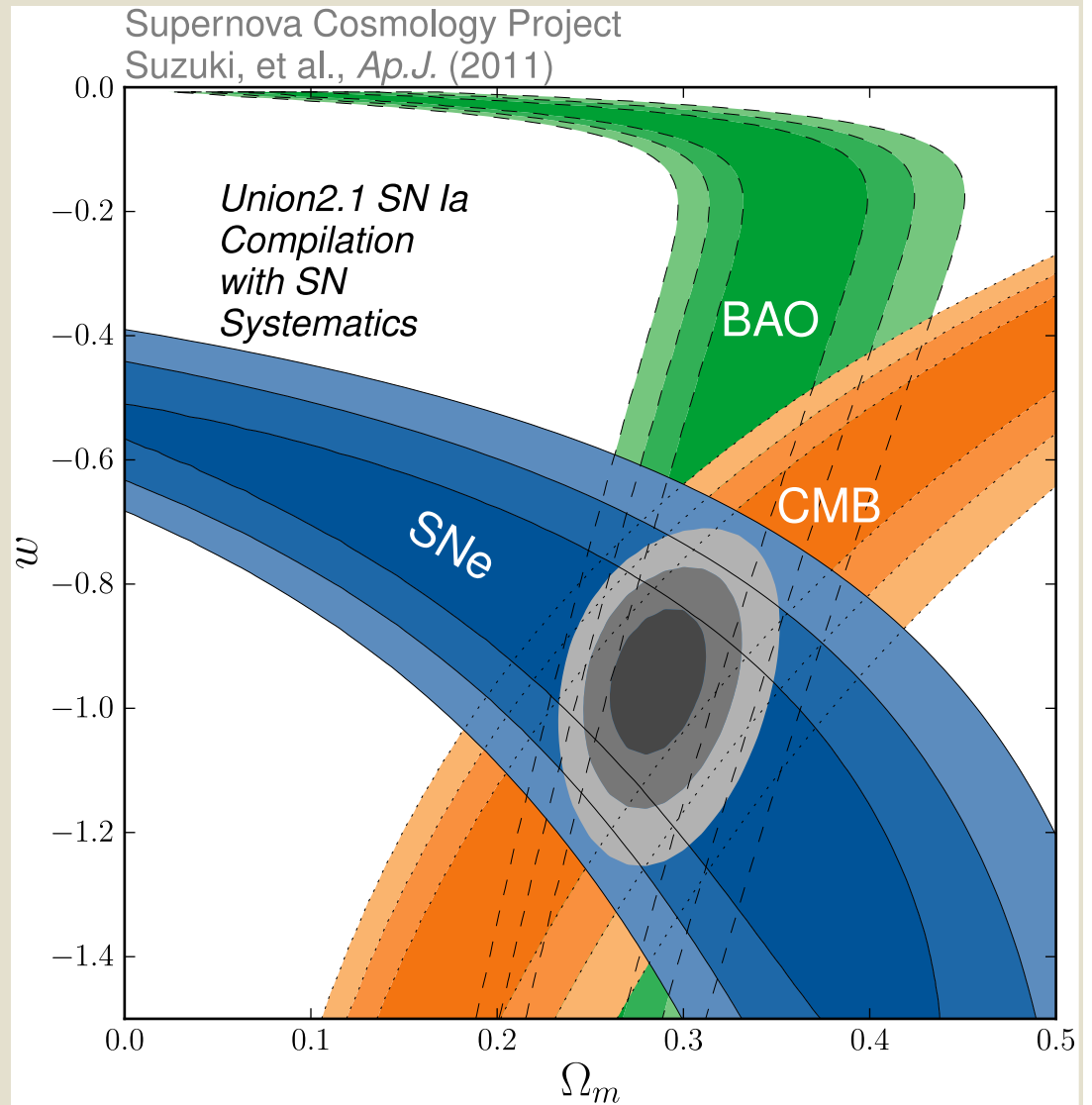
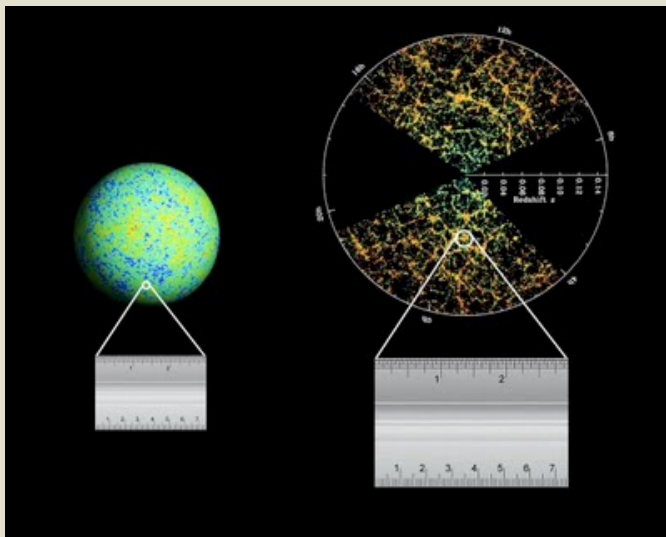


Geometric complementarity gives powerful evidence for dark energy's existence

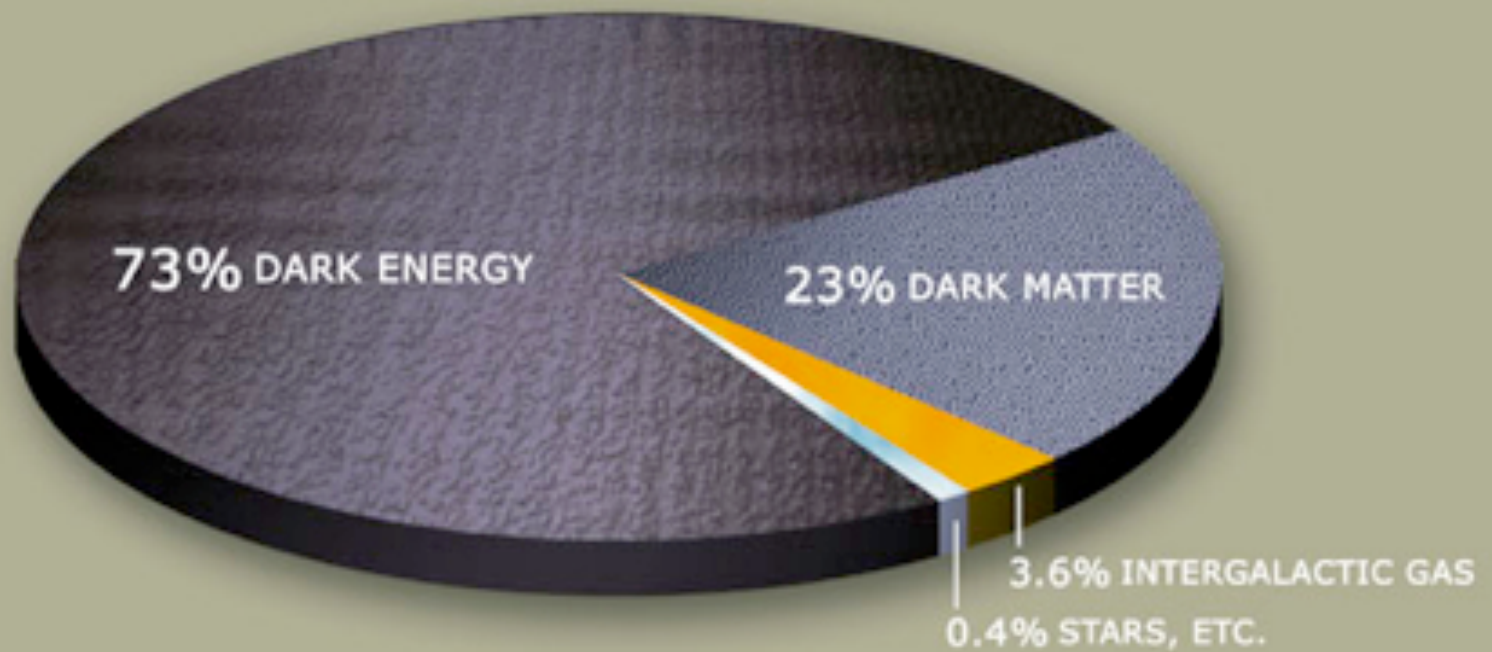
Standard candles



Standard rulers



The concordance cosmological model



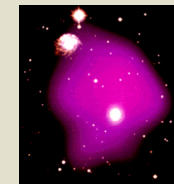
Understanding cosmic acceleration

Cosmic acceleration = a modification of Einstein's equations

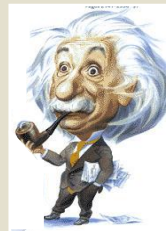


Deviations from GR?

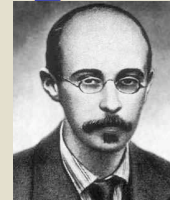
$$G_{\mu\nu} = 8\pi G T_{\mu\nu}$$



New matter?
interactions?



Λ ?



Inhomogeneous universe?

Broad aim = Phenomenology
Distinguish which sector: new gravity, new matter or Λ ?

Ambitious aim = Theoretical model
Learn something more about the underlying theory?

Ways to modify gravity?

- Scalar tensor gravity = simple models we can model effects for

GR

$$S = \int d^4x \sqrt{-g} \frac{1}{16\pi G} R.$$

f(R) gravity

$$S = \int d^4x \sqrt{-g} \frac{1}{16\pi G} (R + f_2(R))$$

Scalar tensor gravity

$$S = \int d^4x \sqrt{-g} \frac{1}{16\pi G} f_1(\phi) R.$$

Higher dimensional gravity e.g. DGP

$$S = \int d^5x \sqrt{-g^{(5)}} \frac{1}{16\pi G^{(5)}} R^{(5)}$$

- Active area of research, many different options, no solutions, yet
- Common theme: A scalar degree of freedom

Alternative explanations to expansion history

- Alter Friedmann and acceleration equations at late times

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3}(\rho_m + 3P_m) + \textit{stuff}$$

or

$$\textit{stuff} + \frac{\ddot{a}}{a} = -\frac{4\pi G}{3}(\rho_m + 3P_m) \quad ?$$

e.g. f(R) gravity

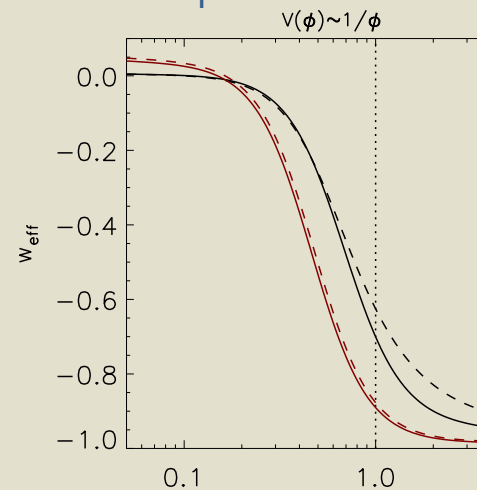
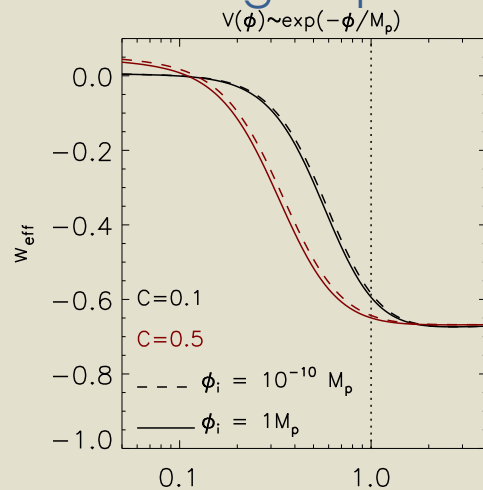
$$-H^2 f_R + \frac{a^2}{6} f + \frac{3}{2} H \dot{f}_R + \frac{1}{2} \ddot{f}_R + \frac{\ddot{a}}{a} = -\frac{4\pi G}{3}(\rho + 3P)$$

e.g. DGP gravity

$$-\frac{\dot{H}}{r_c} + \frac{\ddot{a}}{a} = -\frac{4\pi G}{3}(\rho + 3P)$$

Palatable and unpalatable attraction...

- Attractor solutions give predictions independent of initial conditions,



RB, Flanagan, Laszlo, Trodden 2008

- for better or worse^a e.g. $f(R)$ Amendola et al 2007
- Can evade (unpalatable) attractors, by retrofitting Λ CDM background, but at the high price of more fine-tuning
 - e.g. $f(R)$ Hu and Sawicki 2007

$$f(R) = -m^2 \frac{c_1 (R/m^2)^n}{c_2 (R/m^2)^n + 1},$$

Can we tie data a step closer to theory?

- What observational properties might the most general action predict?

$$S = \int d^4x \sqrt{-g} \left\{ \frac{M_p^2}{2} R - \frac{1}{2} (\nabla\phi)^2 - V(\phi) \right.$$

Canonical scalar field

Quartic kinetic

$$+ f_{quartic}(\phi) (\nabla\phi)^4$$

Coupling to curvature

$$+ f_{curv}(\phi) G^{\mu\nu} \nabla_\mu \phi \nabla_\nu \phi$$

Gauss-Bonnet (GB) term

$$+ f_{GB}(\phi) (R^2 - 4R^{\mu\nu} R_{\mu\nu} + R_{\mu\nu\sigma\rho} R^{\mu\nu\sigma\rho}) \}$$

$$+ S_m \left[e^{\alpha(\phi)} g_{\mu\nu} (1 + f_{kin}(\phi) (\nabla\phi)^2), \psi_m \right]$$

Non-minimally coupling to matter

Attractor behaviors

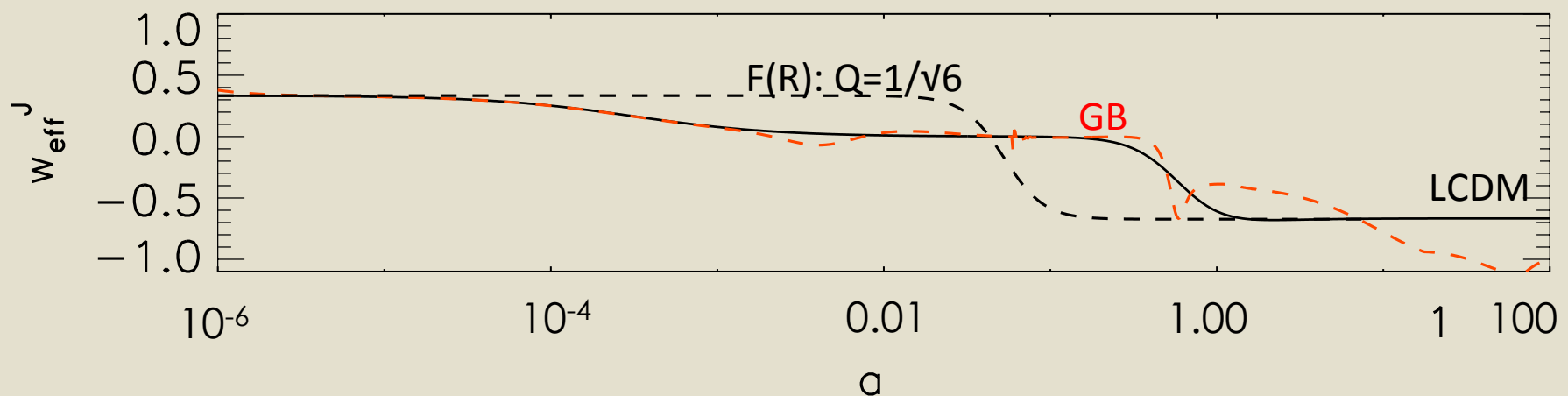
- Simple forms for couplings/interactions yield a small set of predictions

Attractor	Ω_ϕ	w_ϕ	w_E	w_J
MAT- λ	$\frac{3(1+w_m)}{\lambda^2}$	w_m	w_m	$\frac{w_m + \sqrt{6}Qx/3}{1 - \sqrt{6}Qx}$
MAT - Q	$\frac{2Q^2}{3}$	1	$\frac{2Q^2}{3}$	$\frac{4Q^2}{3(1-2Q^2)}$
ACC- λ	1	$-1 + \frac{\lambda^2}{3}$	$-1 + \frac{\lambda^2}{3}$	$-1 + \frac{\lambda^2 - 2Q\lambda}{3(1-Q\lambda)}$
ACC - GB	1	-1	-1	-1

$$V = V_0 \exp\left(-\lambda \frac{\phi}{M_p}\right)$$

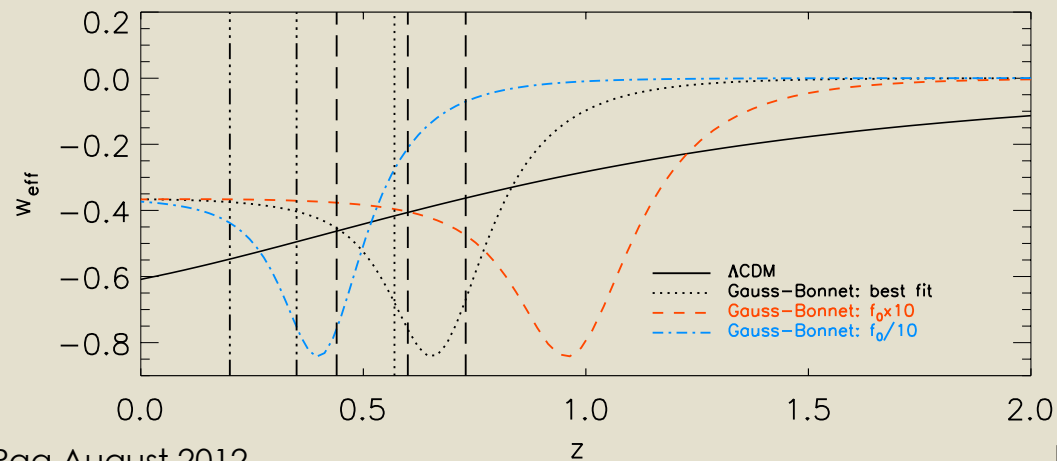
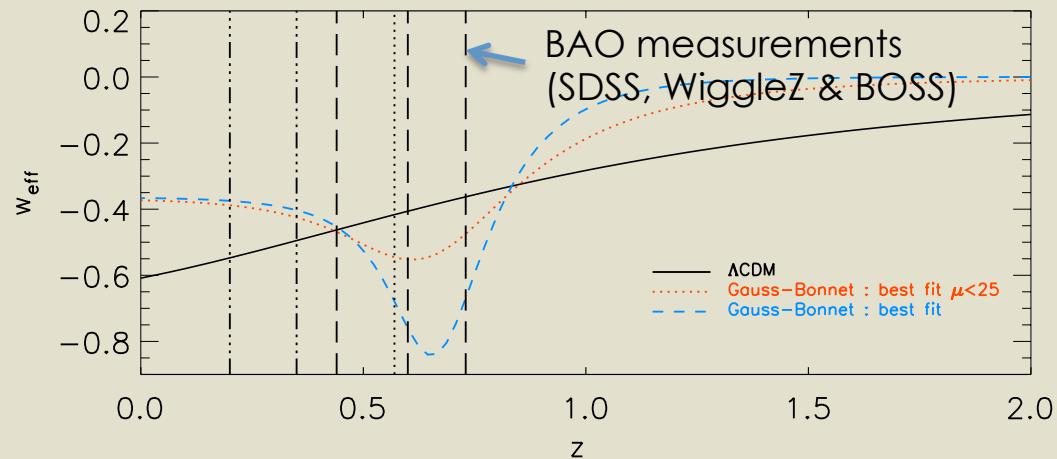
$$e^\alpha = \exp\left(-2Q \frac{\phi}{M_p}\right)$$

$$f_{GB} = F_0 \exp\left(-\mu \frac{\phi}{M_p}\right)$$



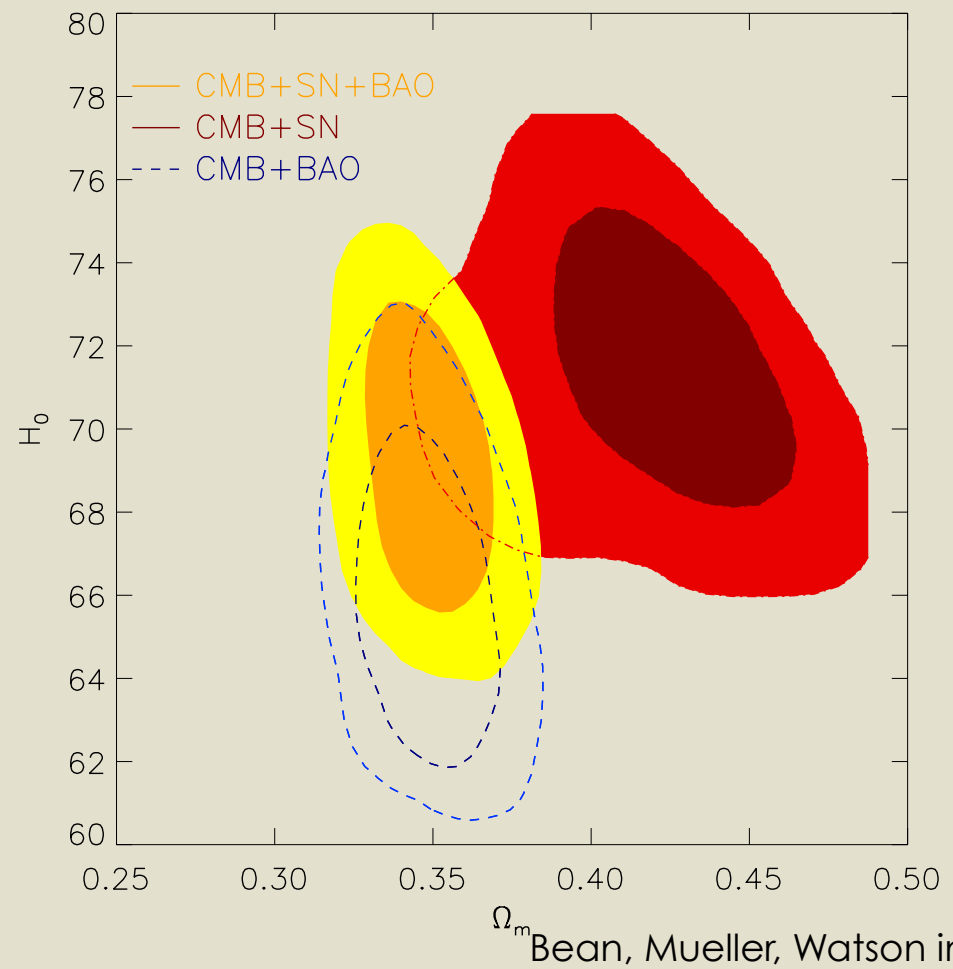
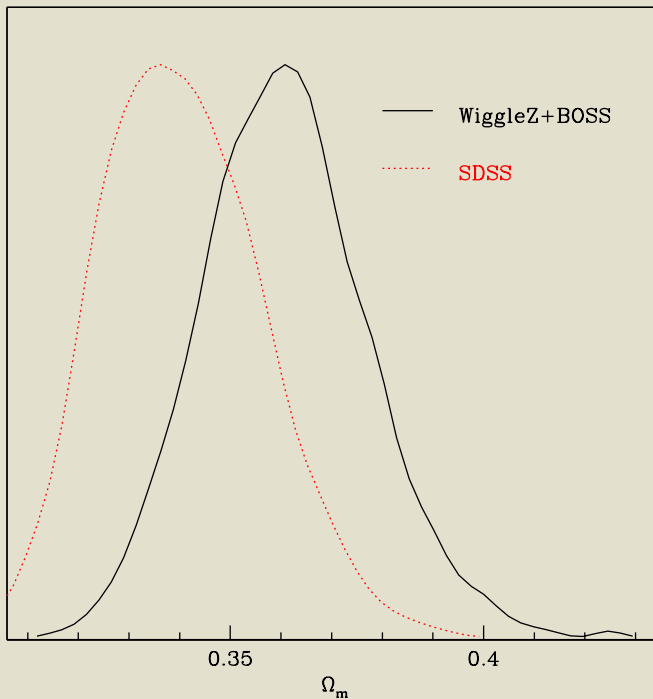
The power of multi-epoch measurements

- BAO and SN data give multiple tests of cosmic dynamics



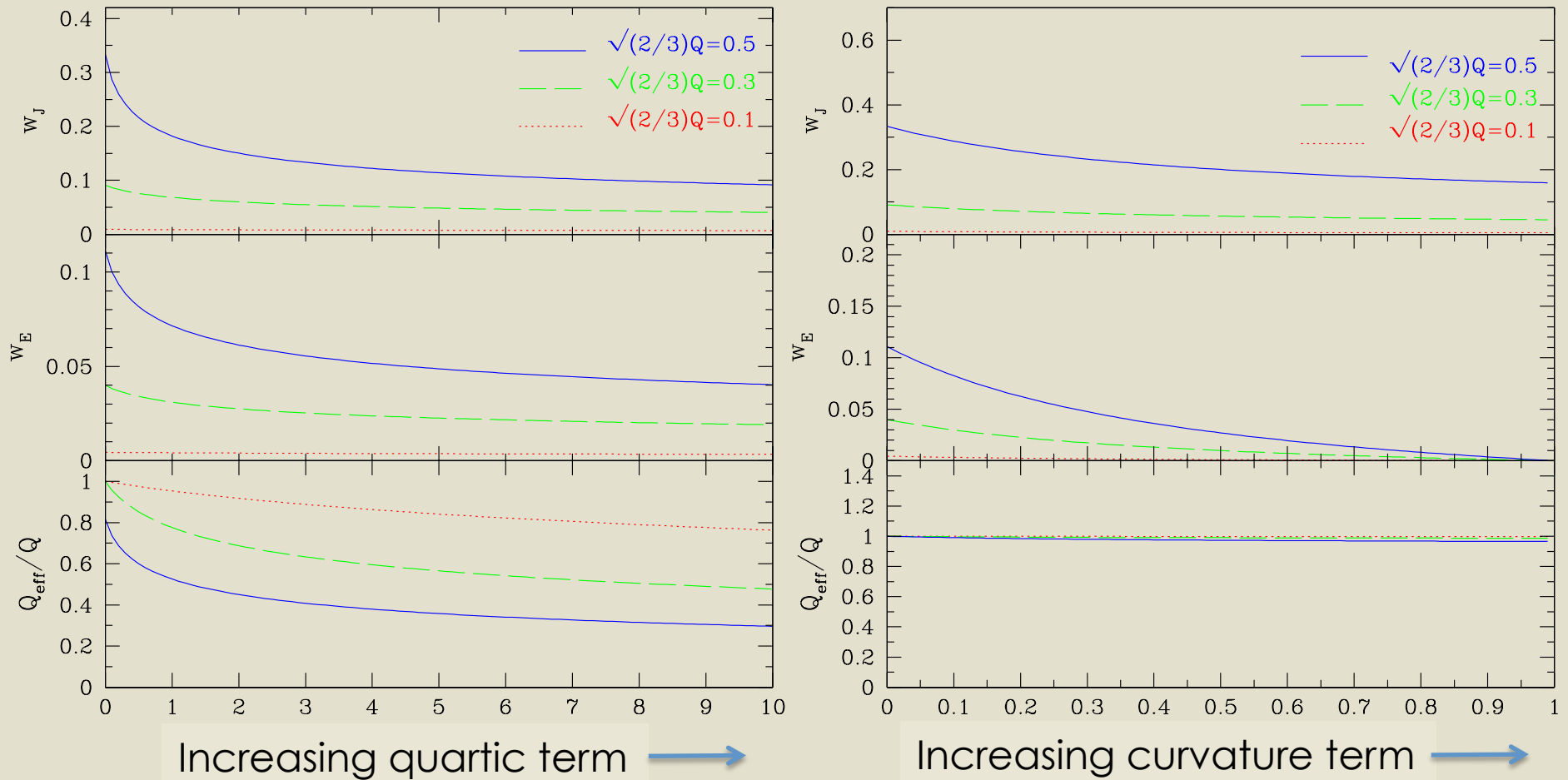
The power of multi-epoch measurements

- In combination, rule out Gauss-Bonnet term: $\Delta\chi^2(\text{GB-LCDM})=+17$



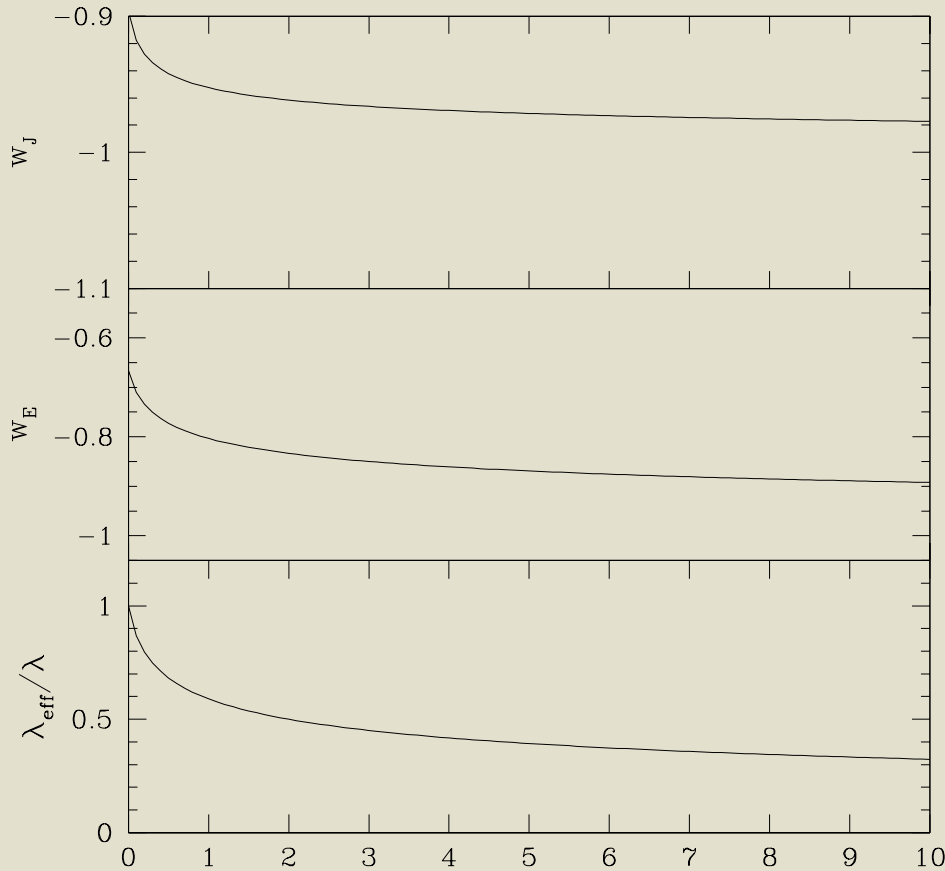
Quartic and curvature interactions have cosmologically interesting effects

Matter dominated era

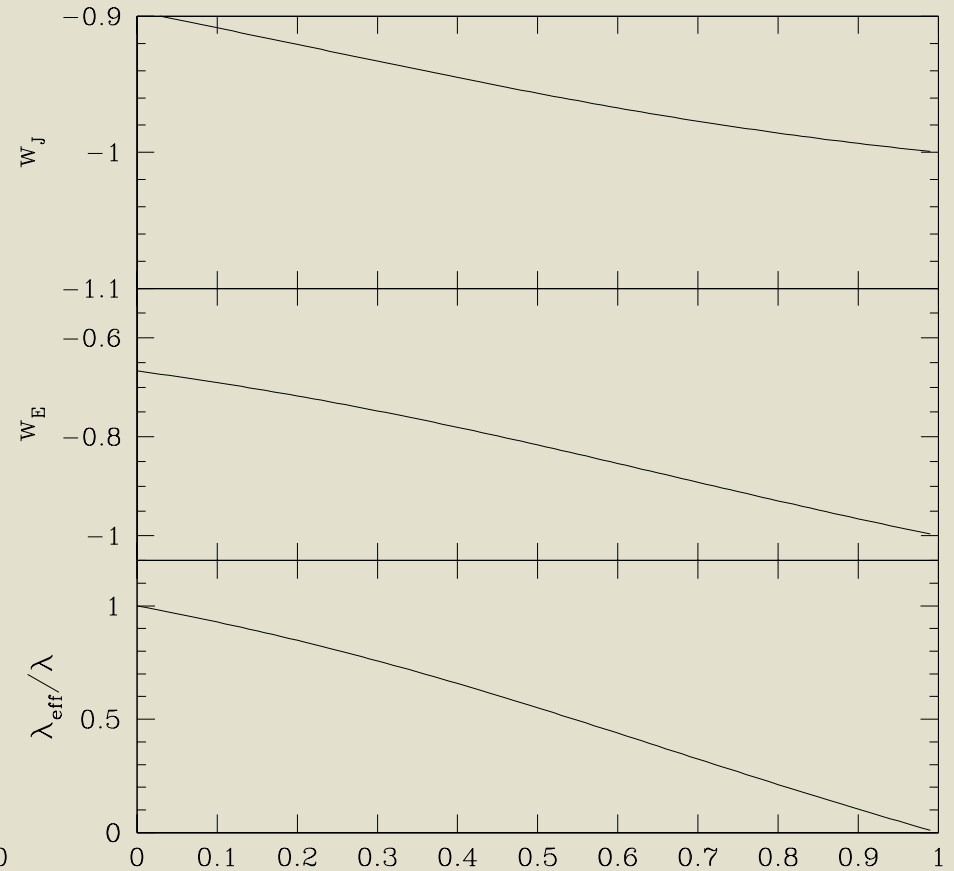


Quartic and curvature interactions have cosmologically interesting effects

Late time accelerating era

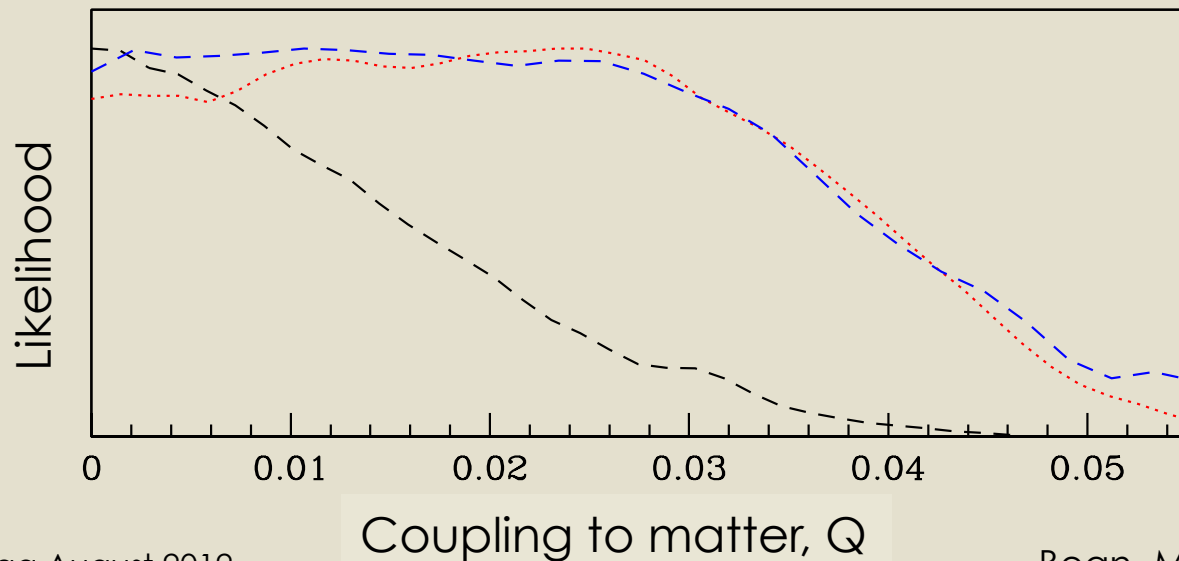
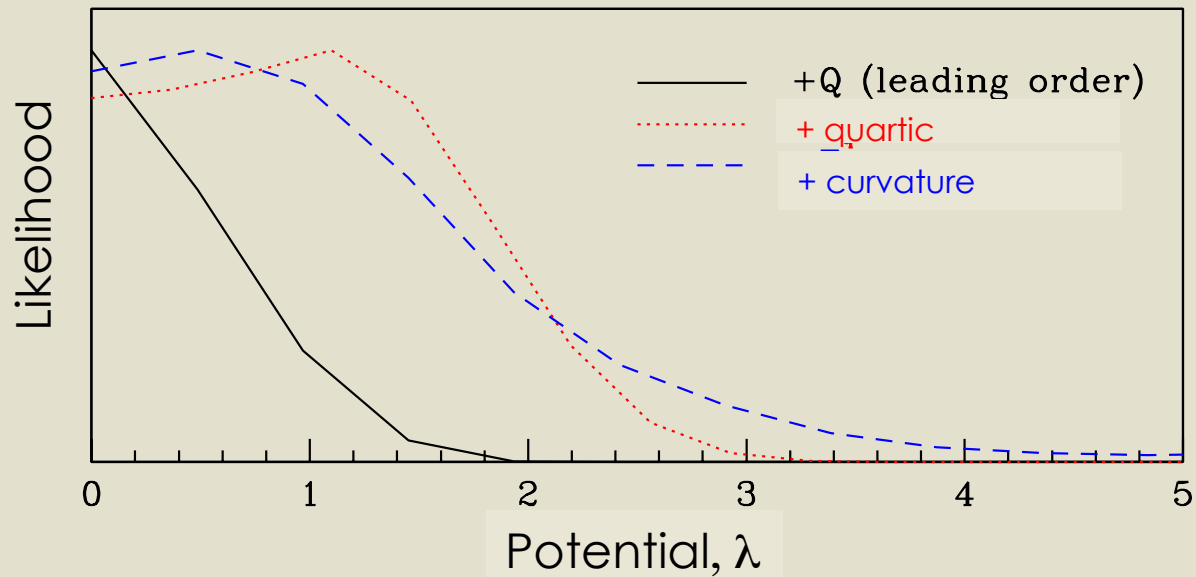


Increasing quartic term \rightarrow



Increasing curvature term \rightarrow

Geometric cosmological constraints



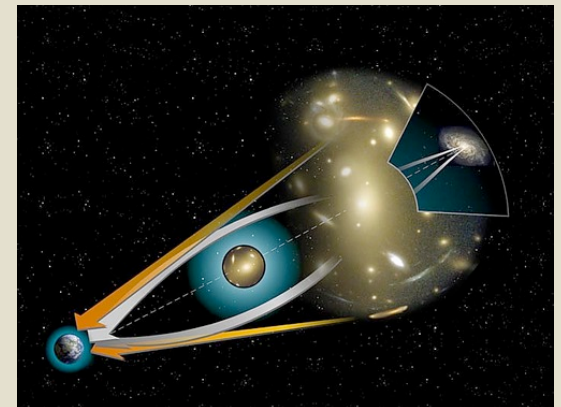
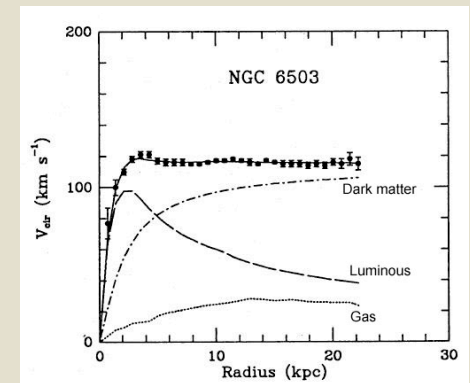
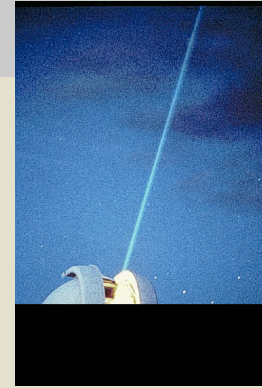
There are always benefits to asking more questions...



Rachel Bean: PhysPag August 2012

Weak field tests of gravity

- Terrestrial and Solar System
 - Lab tests on mm scales
 - Lunar and planetary ranging
- Galactic
 - Galactic rotation curves and velocity dispersions
 - Satellite galaxy dynamics
- Intergalactic and Cluster
 - Galaxy lensing and peculiar motions
 - Cluster dynamical, X-ray & lensing mass estimates
- Cosmological
 - Early times: BBN, CMB correlations
 - Late times: Large scale structure



Three groups of extra galactic observations for testing gravity

I: Background expansion

CMB angular diameter distance

Supernovae luminosity distance

BAO angular/radial scale

II: Growth, up to some normalization

Galaxy autocorrelations

Galaxy – ISW x-corrln

Xray and SZ galaxy cluster measurements

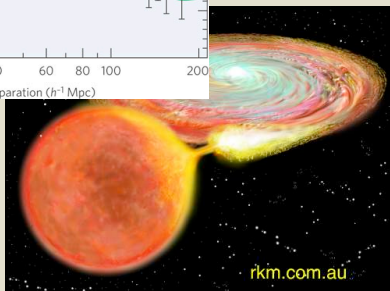
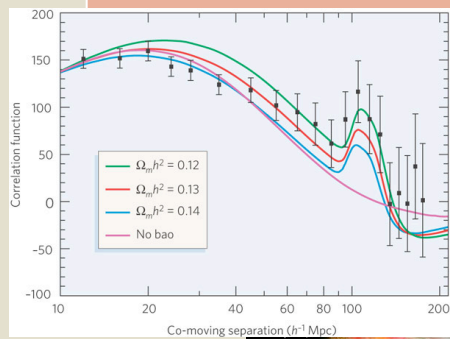
Ly-alpha measurements

III: Growth directly

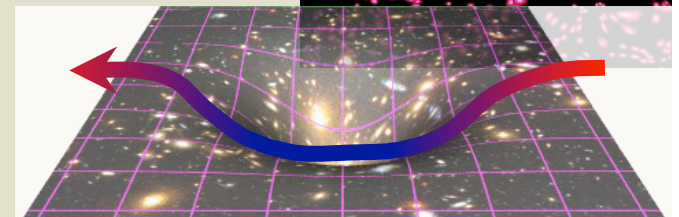
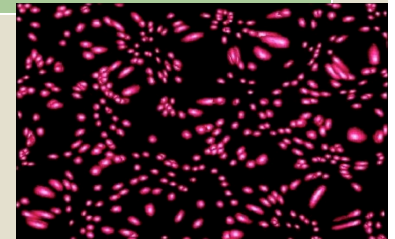
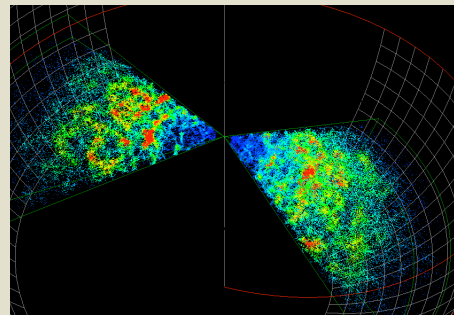
CMB ISW autocorrelation

Weak lensing autocorrelation

Peculiar velocity distribution/
bulk flows



rkm.com.au



Phenomenological model of gravity

- Perturbed metric $ds^2 = -(1 + 2\psi)dt^2 + a^2(1 - 2\phi)dx^2$
- Aim to describe phenomenological properties common to theories

- A modification to Poisson's equation, Q

$$k^2 \phi = -4\pi G Q a^2 \rho \Delta$$

$Q \neq 1$: can be mimicked by additional (dark sector?) clustering/matter

- An inequality between Newton's potentials, R

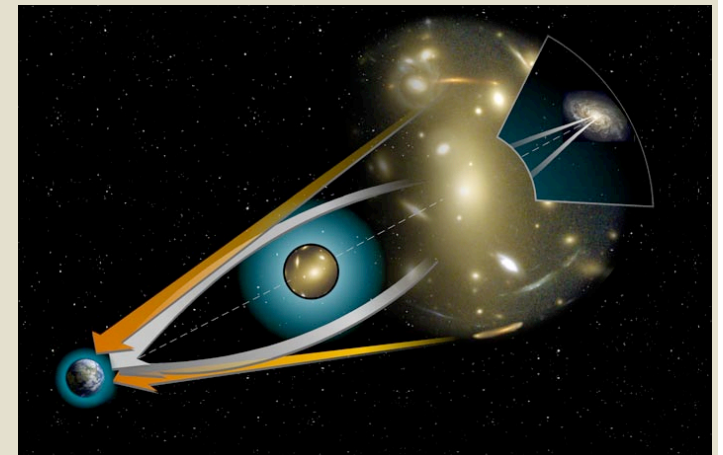
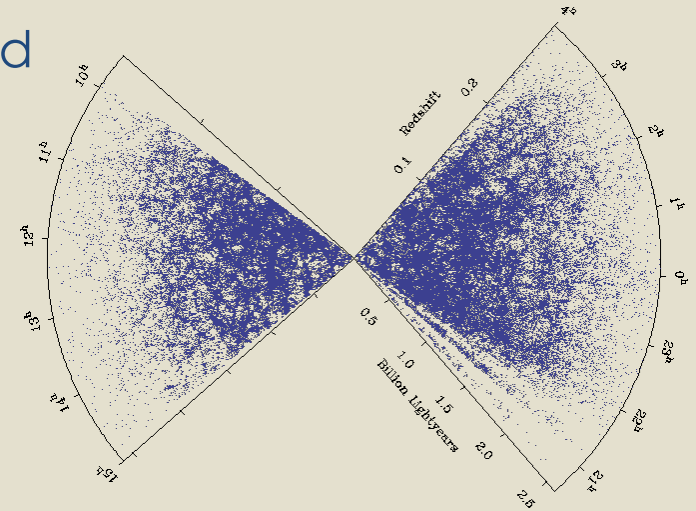
$$\psi = R\phi$$

$R \neq 1$: not easily mimicked.

- potential smoking gun for modified gravity?
- Significant stresses exceptionally hard to create in non-relativistic fluids e.g. DM and dark energy.

Complementary tests of gravity

- Non-relativistic tracers: Galaxy positions and motions
 - Measure $\psi \sim G_{\text{mat}} = QRG_N$
 - Biasing of tracer (galaxy) issue
- Relativistic tracers: Weak lensing and CMB
 - Sensitive to $(\phi+\psi) \sim G_{\text{light}} = Q(1+R)G_N$
 - Direct tracer of potential, but still
 - stochasticity relating lensing and surveyed galaxies
 - plenty of systematics (photo-z, IAs...)
- Contrasting tracers are the key to understanding gravity



Putting it all in the mix

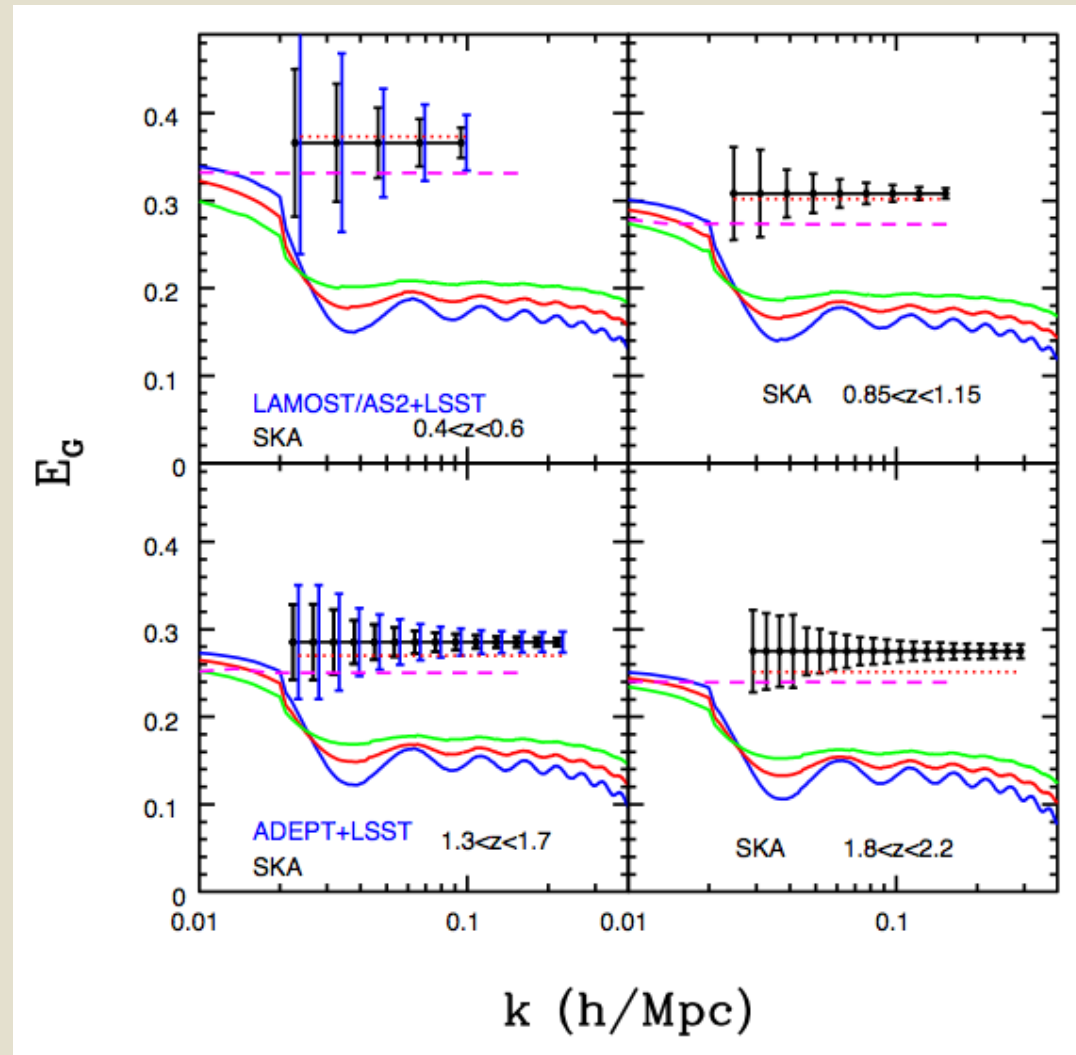
- A “smoking gun” for GR on cosmic scales

$$E_G \sim \frac{\text{galaxy position-lensing correlation } (C_l^{gG})}{\text{redshift space - galaxy position correlation } (C_l^{g\theta})}$$

- Contrasts relativistic and non-relativistic tracers $\Rightarrow R \neq 1$?
 - Lensing: $G \sim \phi + \psi \sim Q(1+R)$,
 - Galaxy position and motion: $g, \theta \sim \psi \sim QR$
- Independent of galaxy bias and initial conditions

$$\frac{C_l^{gG}}{C_l^{g\theta}} \sim \frac{b \sigma_8^2}{b \sigma_8^2}$$

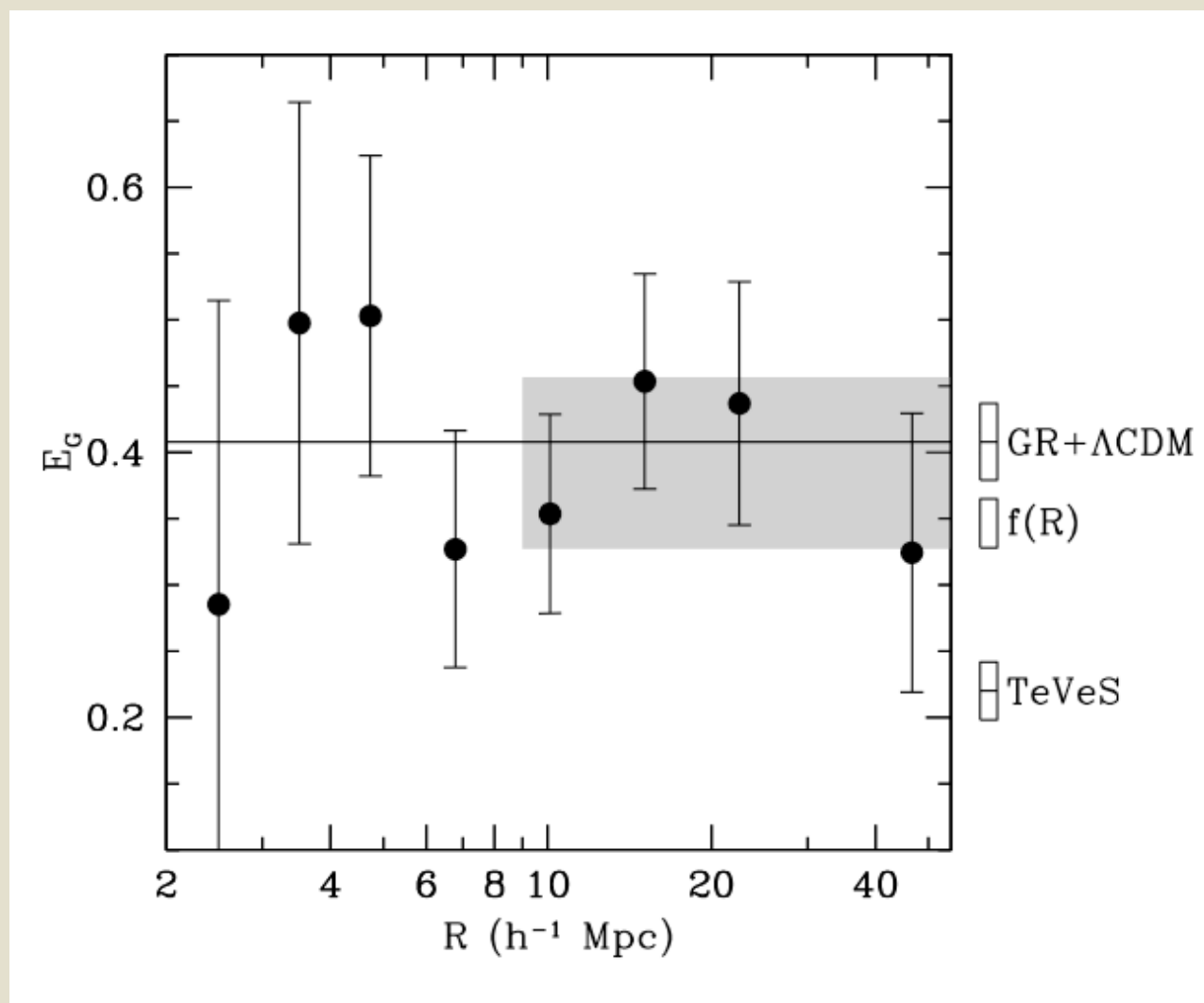
Distinguishing between modified gravity and Λ



$$E_g \sim \frac{C_l^{g\kappa}}{C_l^{g\Theta}}$$

- GR —————
- DGP
- $f(R)$ - - - - -
- TeVeS $K=0.1$ —————
- TeVeS $K=0.09$ —————
- TeVeS $K=0.08$ —————

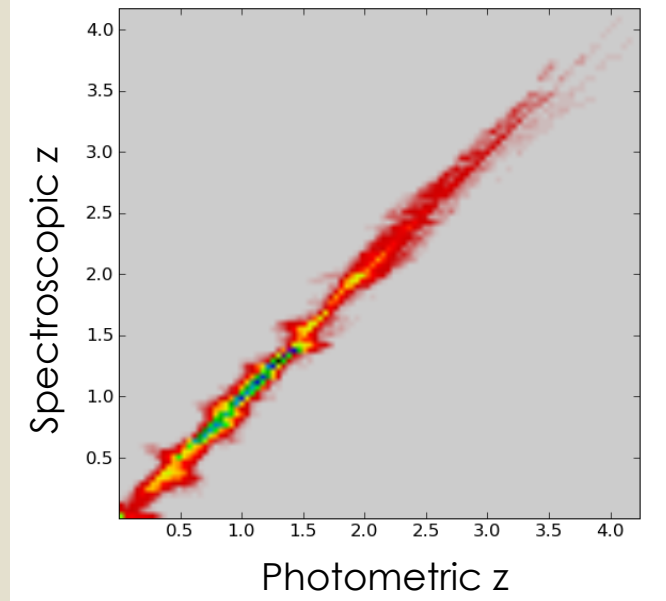
Vital proof of principle with SDSS LRG data



Reyes et al Nature 2010

Complications: photometric redshifts

- Facilitates fast and wide survey
- Enables tomography
 - Measuring evolution on dark energy
 - Cross-correlations between z bins useful for disentangling systematics and cosmology
- But sensitive to modeling
 - galaxy distribution,
 - photo- z statistical accuracy, systematic offsets and catastrophic errors



Credit: LSST Consortium

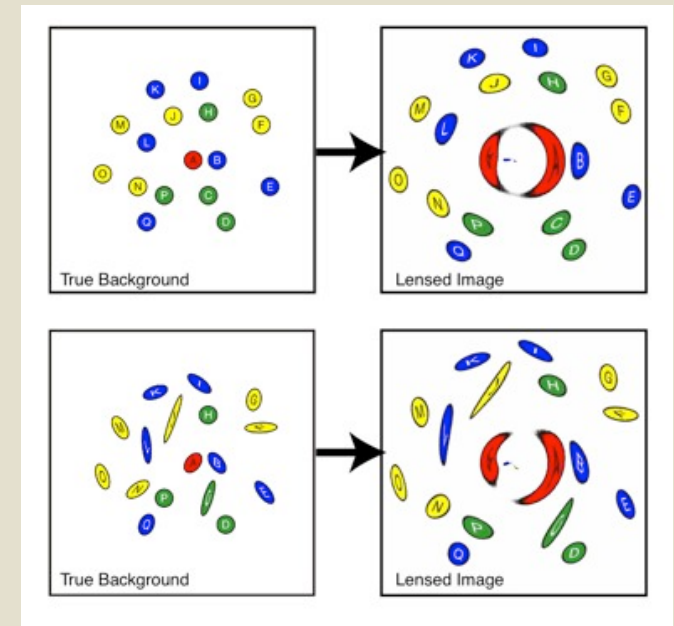


Complications : Intrinsic alignments

- Lensing distortions detected using statistical correlations

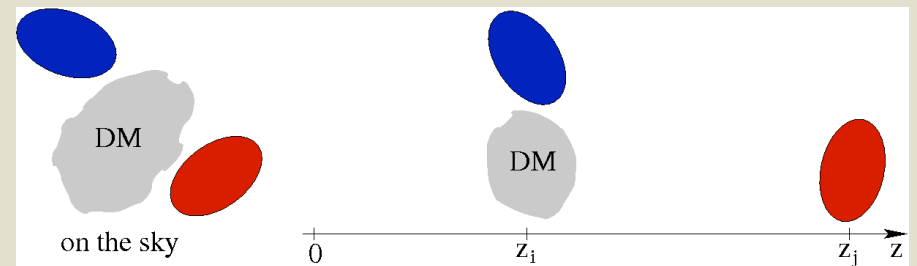
$$\epsilon^i(\theta) = \gamma_G^i(\theta) + \gamma_I^i(\theta) + \epsilon_{rnd}^i(\theta).$$

- Random ellipticity not an issue
- Instrumental & astrophysical “contaminants” introduce systematic shear calibration uncertainties
- Correlated contaminant need to be modeled and disentangled from cosmological shear
 - E.g. Intrinsic galactic alignments



Credit: Williamson, Oluseyi, Roe 2007

Cosmo+Intrinsic shear (anti) correlation

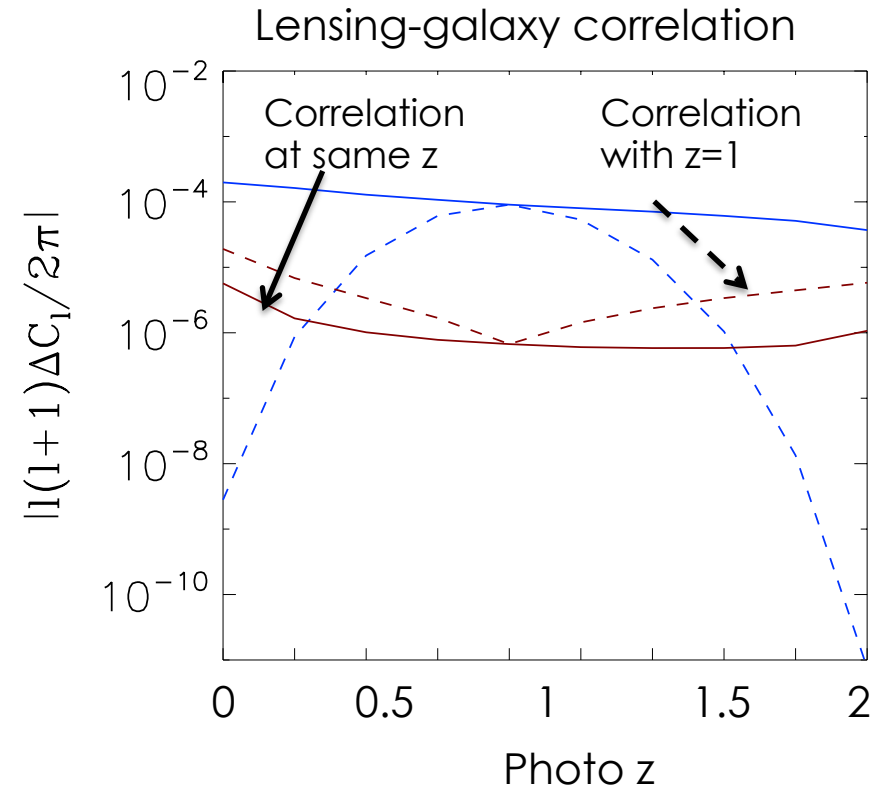
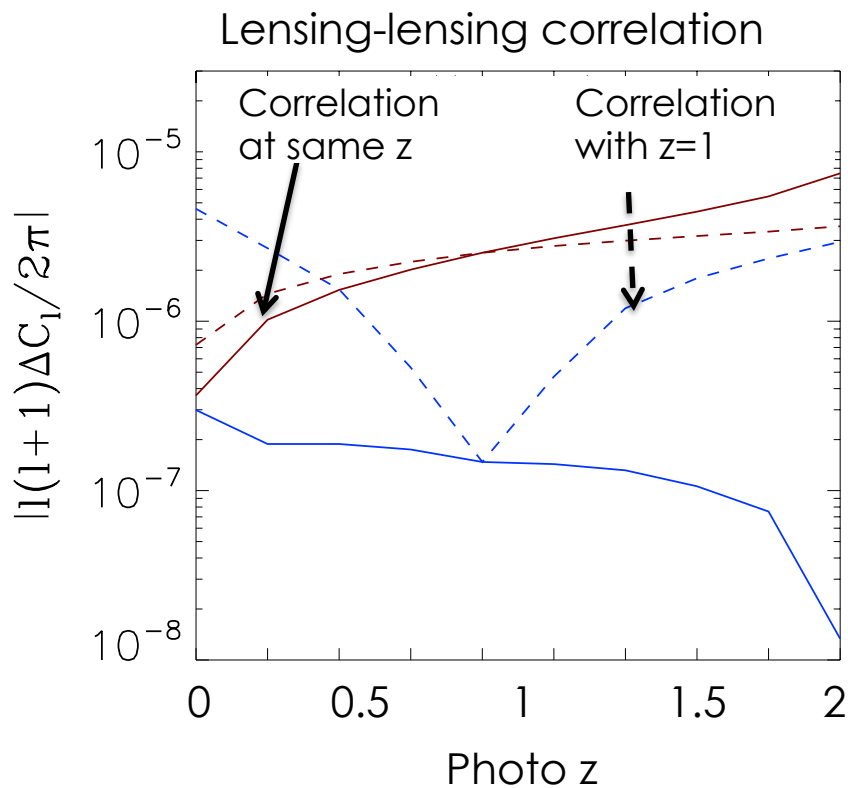


Credit: Benjamin Joachimi, iCosmo

Cross- correlations and tomography

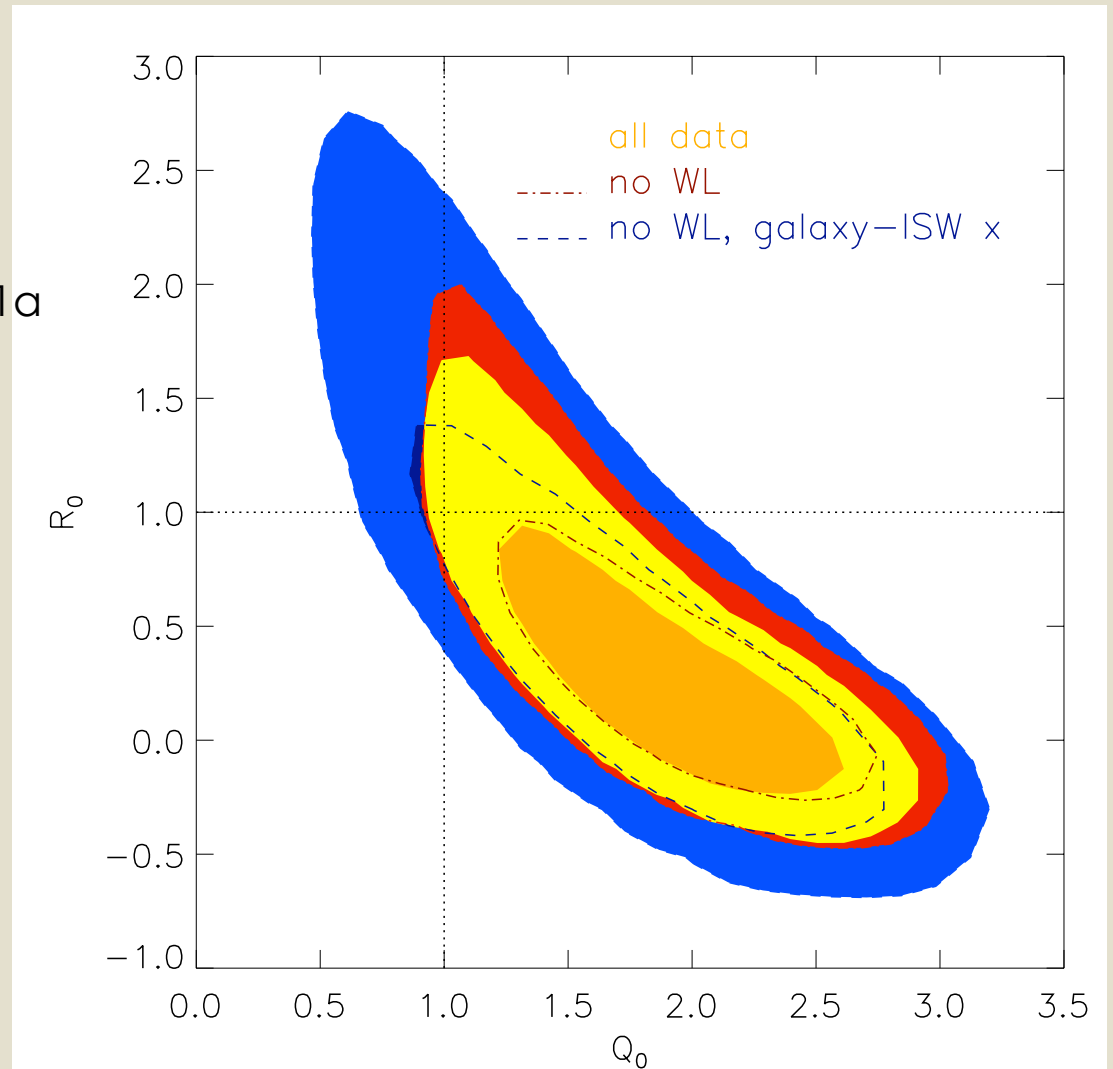
- Use difference in redshift signatures to break degeneracy between systematics and dark energy theory

Differences between **LCDM + sys errors vs no sys** and **MG vs LCDM for lensing and galaxy**



Current constraints

- Multiple data
WMAP CMB, SDSS LRG auto ,
SDSS-WMAP cross correlation,
COSMOS weak lensing, Union SN1a
- CMB-galaxy correlations
give best constraints
- Worst constraint from lensing
+CMB
 - $(\phi+\psi)$ direction $\sim Q(1+R)/2$
- “Figure of Merit”
 - 1/error ellipse area
 - MG FoM ~ 0.03



What about future surveys?

- Fisher matrix analysis = Inverse covariance (error) matrix

$$Cov_{ij}^{-1} = F_{ij} = \frac{\partial t_a}{\partial p_i} Cov_{ab}^{-1} \frac{\partial t_b}{\partial p_j}$$

- Assumed cosmology and parameterization

$$\mathbf{p} = \{\Omega_b h^2, \Omega_m h^2, \Omega_k, \tau, w_0, w_a, Q_0, Q_0(1 + R_0)/2, n_s, \Delta_{\mathcal{R}}^2(k_0), \\ + \text{systematic nuisance parameters}\}$$

- Datasets

$$\mathbf{t} = \{C_{\ell}^{TT}, C_{\ell}^{TE}, C_{\ell}^{EE}, C_{\ell}^{Tg_1}, \dots, C_{\ell}^{Eg_1}, \dots, C_{\ell}^{g_1g_1}, C_{\ell}^{g_1g_2}, \dots, C_{\ell}^{\kappa_{N_{ph}} \kappa_{N_{ph}}}\}$$

- Survey specifications

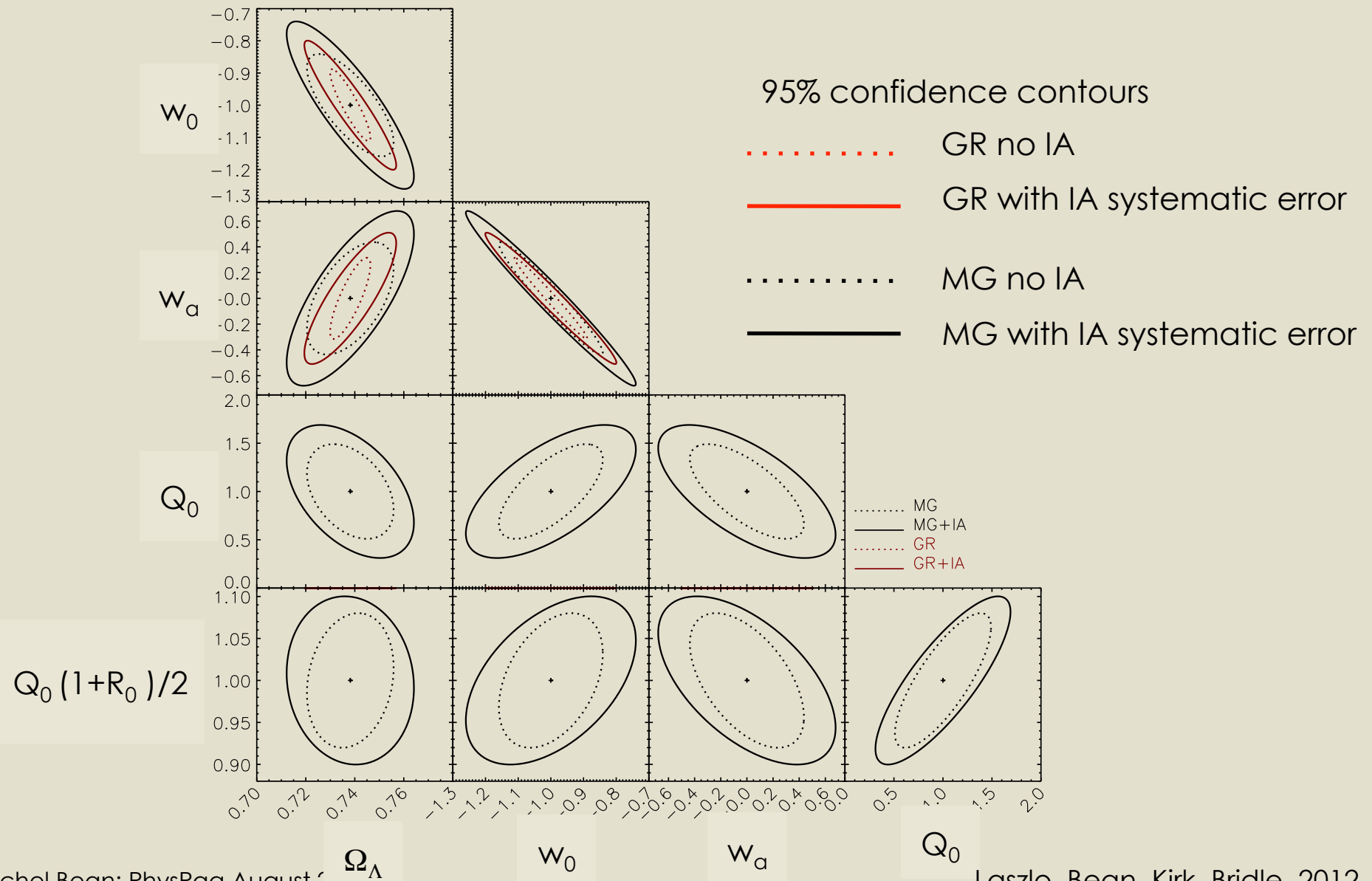
- near future (stage III) and end of decade (stage IV) surveys
- Stage III = Planck CMB + DES-like imaging + BOSS spectroscopic surveys
- Stage IV = Planck CMB + EUCLID-like imaging and spectroscopy

Forecasting: what you put in=what you get out

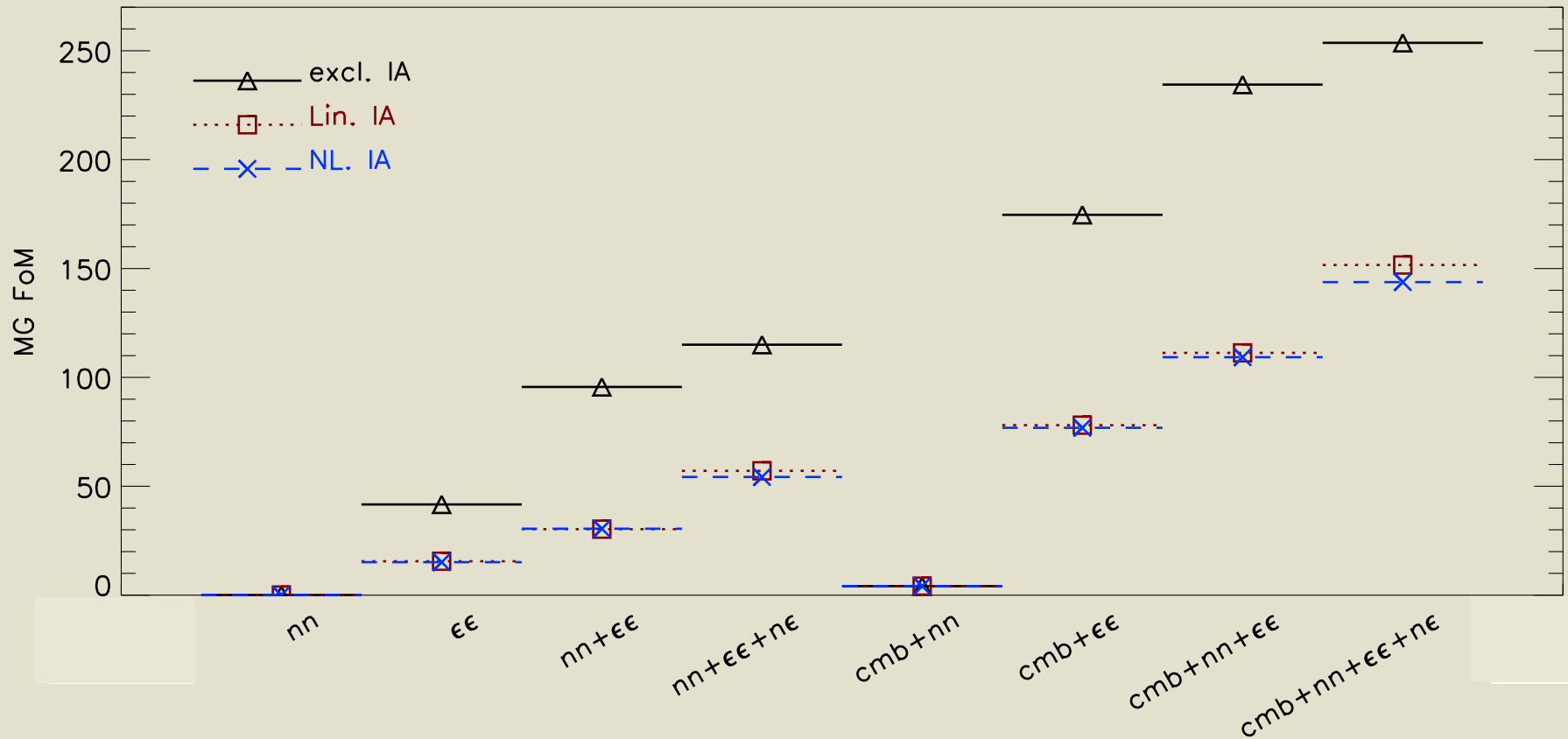
- Figures of merit /Fisher insightful but
- Model dependent – e.g. w_0/w_a or functions of z ?
- Systematic errors difficult but important!
 - Instrumental e.g. calibration uncertainties
 - Internal cross-checks: inter-filter, concurrent & repetition \neq redundancy
 - Modeling: e.g. Photo z modeling errors, nonlinearity
 - Access to ground based facilities,
 - Training sets, simulation suites
 - Astrophysical: e.g. IAs , $H\alpha$ z distribution, galaxy bias, baryonic effects
 - At what scale should one truncate the analysis?
 - Analytical modeling, gridded k & z bins, simulations?
- Buyer beware!
 - risky to compare FoM unless apples-for-apples treatment



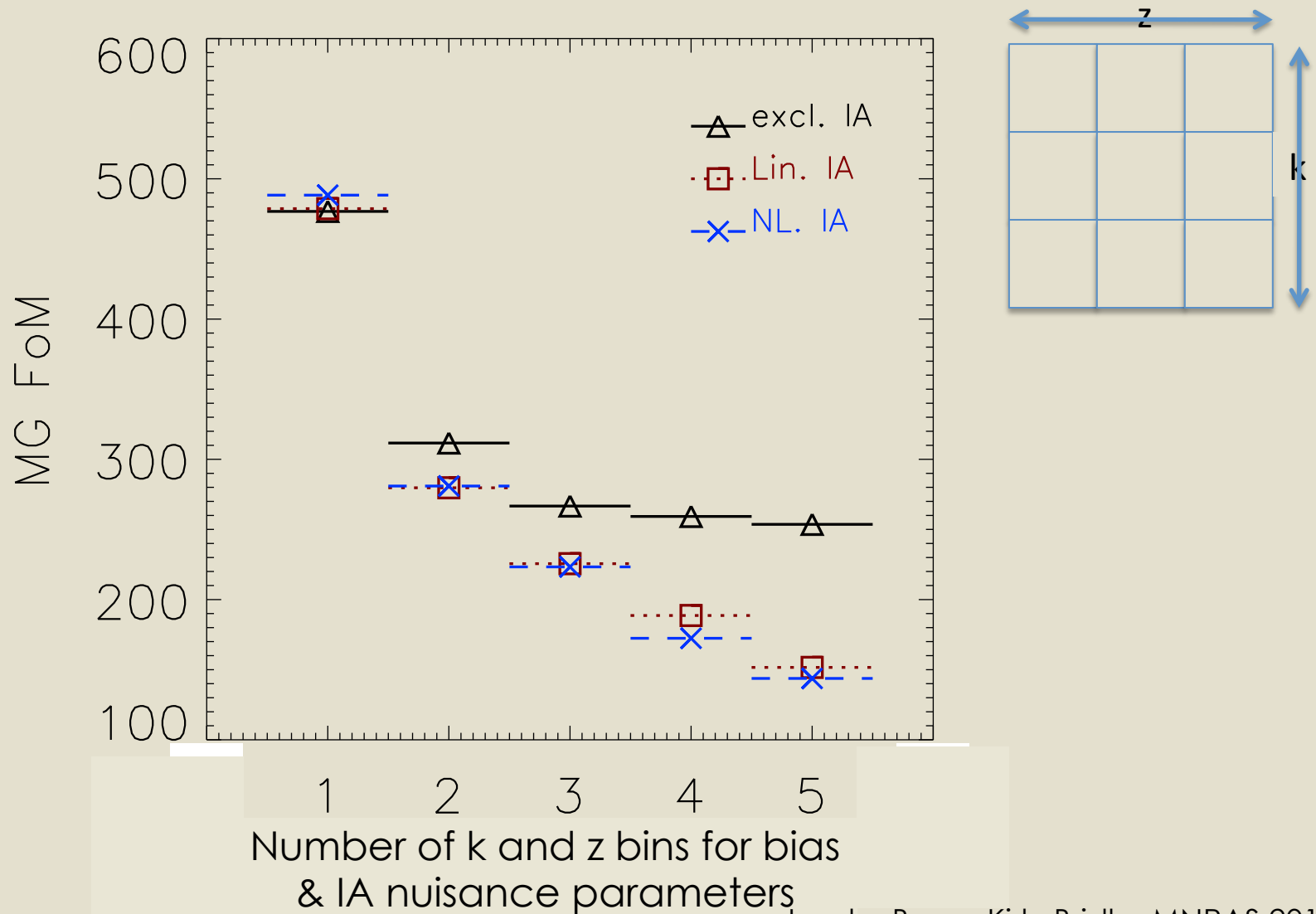
Sensitivity to theory and systematics



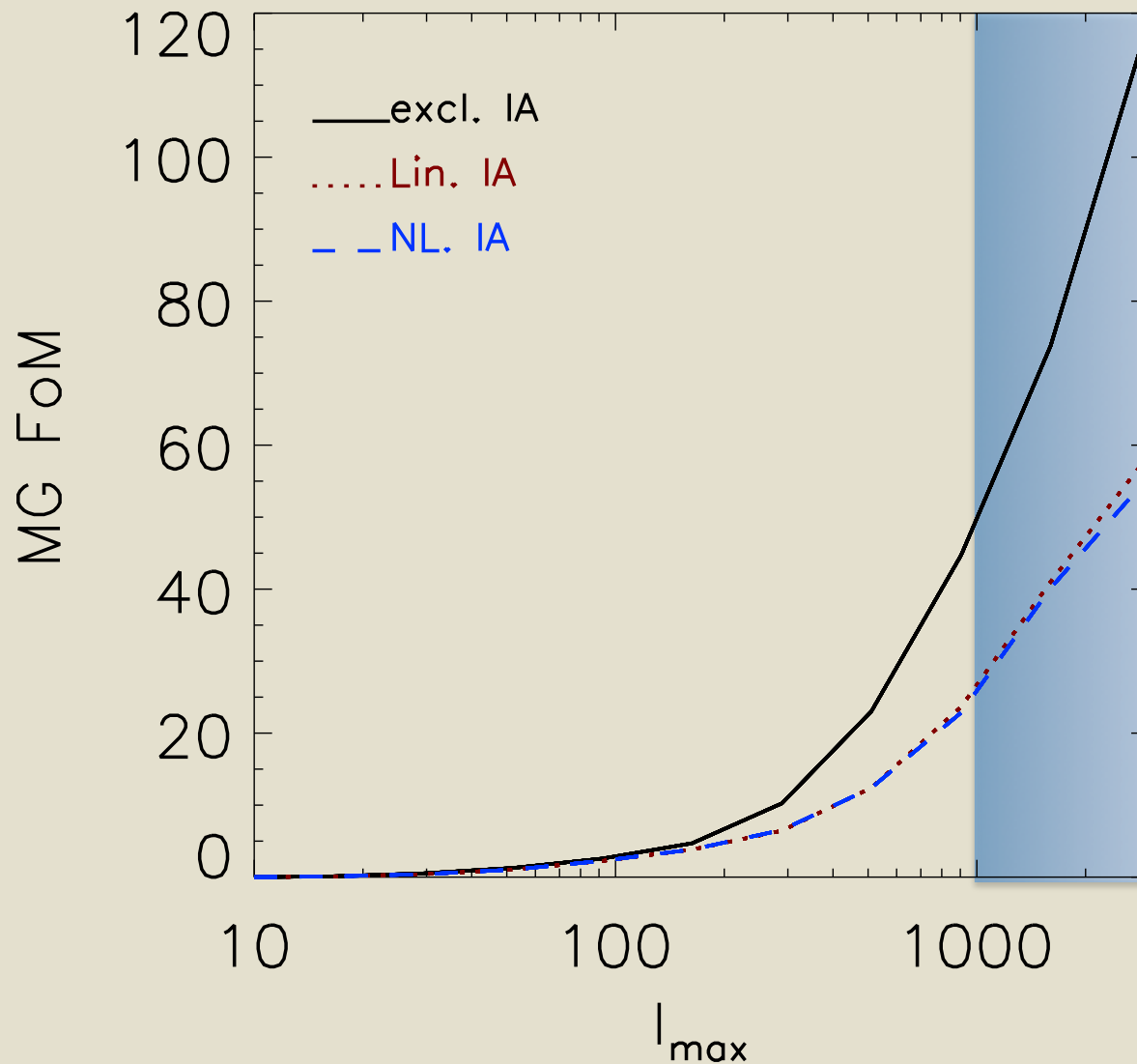
Impact of cross-correlations: reducing systematics, breaking theory degeneracies



Our level of understanding about bias and IA is important



If you understand non-linear scales
they could make a big difference



On scales \lesssim a few Mpc

- Baryonic effects?
- Non-linear modeling?
- Screening effects?

Include small scale modeling uncertainties in forecasts.

Concluding thoughts

- Invaluable opportunity to test the origins of cosmic acceleration and weak field gravity on cosmic scales
 - Theoretical developments, fast evolving.
 - General effective field theory for DE a useful phenomenological approach, with interesting implications for both expansion history and growth history
- Multiple, complementary astrophysical tracers key to finding DE origin
 - geometric techniques important record of expansion history
 - relativistic & non-relativistic LSS tracers distinguish gravity's properties
 - Surveys will give us information across z and from horizon to sub-halo scales
- Honest assessment of systematics essential
 - Theory and systematics can be tightly coupled.
 - Can significantly impact predictions (beware apples vs oranges)
 - Survey and algorithm development + x-corr key to mitigate these.
- FoMs useful but a high pass filter on data. Mapping to the underlying theory is the ultimate goal.